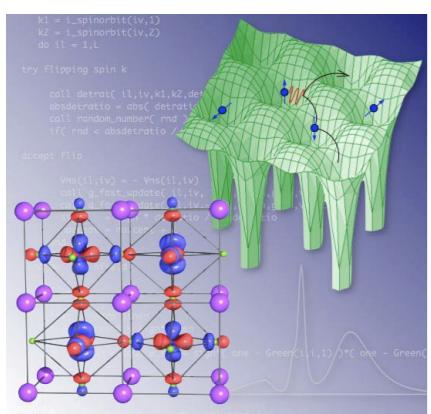
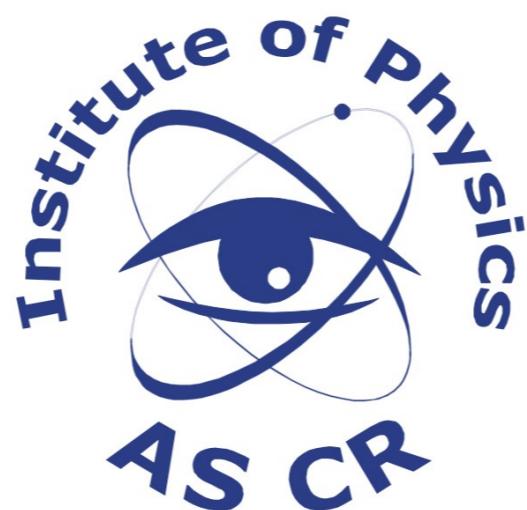


# Spin transitions in strongly correlated materials

Jan Kuneš



DFG FOR 1346  
Dynamical Mean-Field Approach with Predictive Power for Strongly Correlated Materials  
&  
GA CR P204/10/0284

# Collaborators

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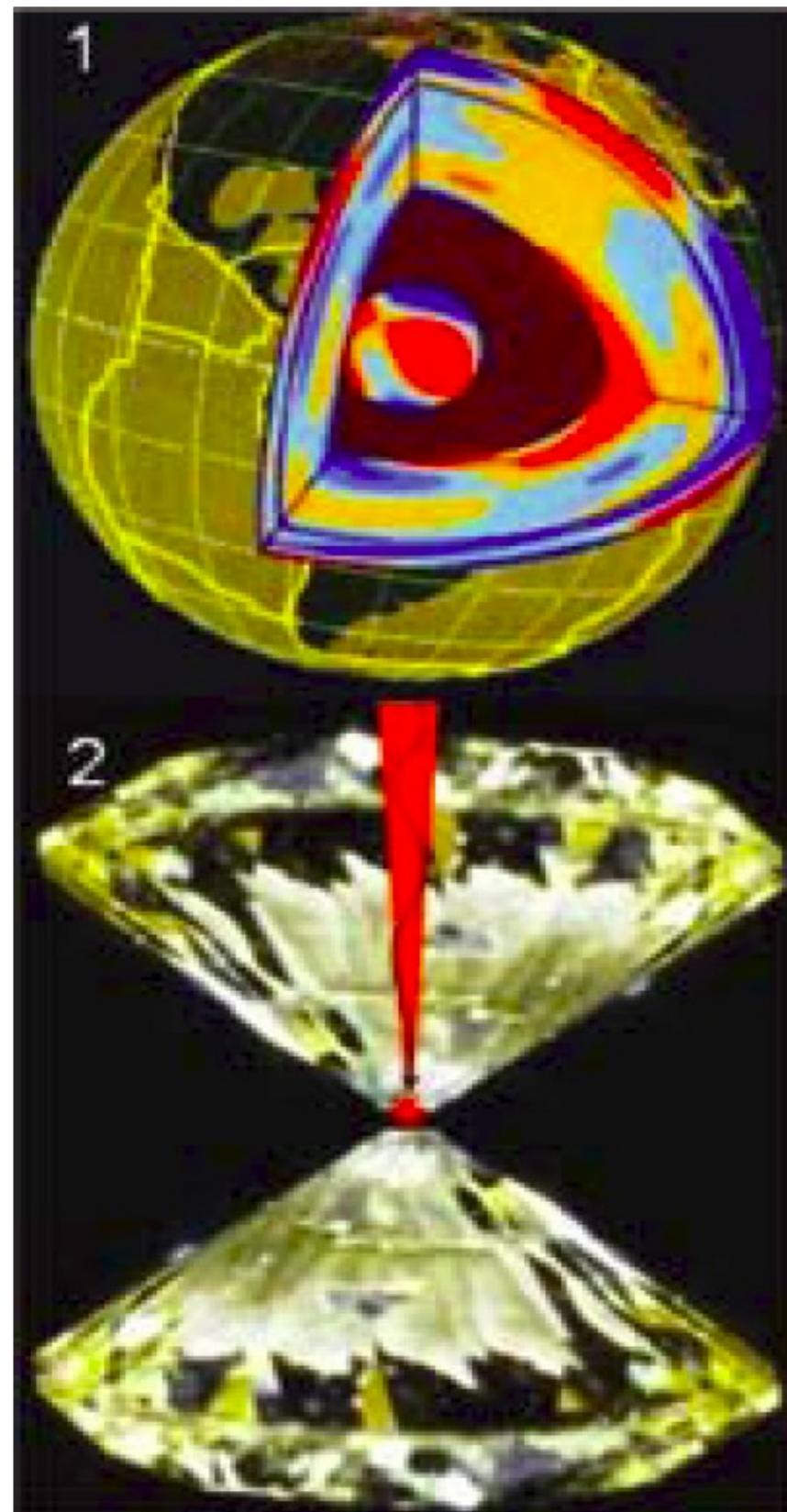
W. E. Pickett, R. T. Scalettar

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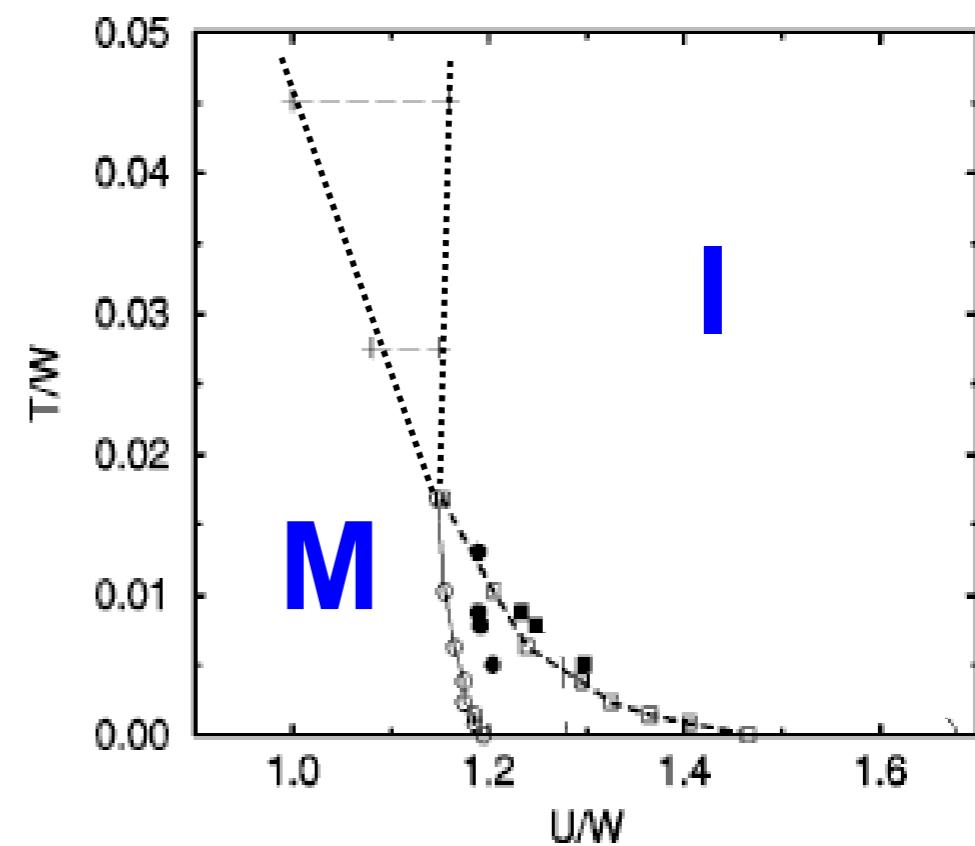
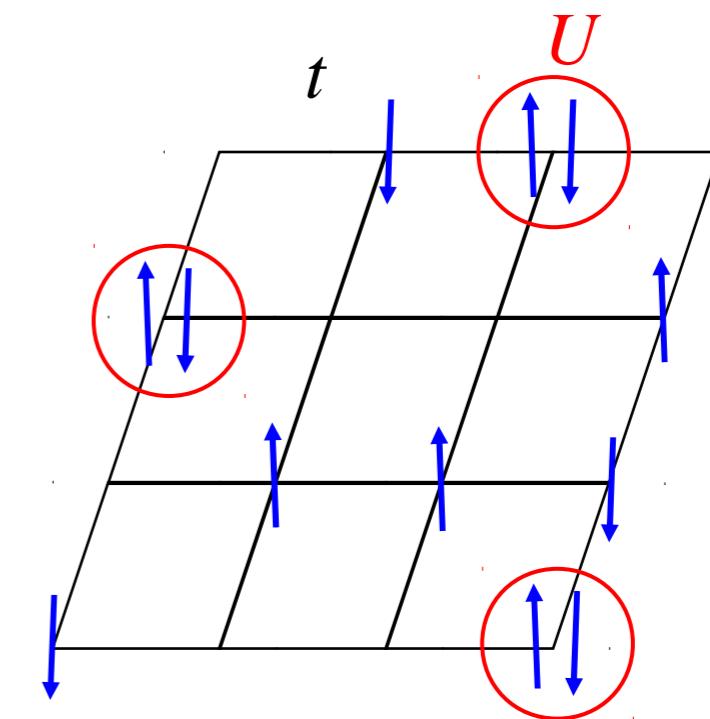
# Outline

- HS-LS transitions in models and materials
- Pressure-driven transition:  $\text{MnO}$ ,  $\text{Fe}_2\text{O}_3$
- HS/LS degeneracy:  $\text{LaCoO}_3$
- Blume-Emery-Griffiths model in fermionic systems
- From cobaltites to manganites
- Conclusions

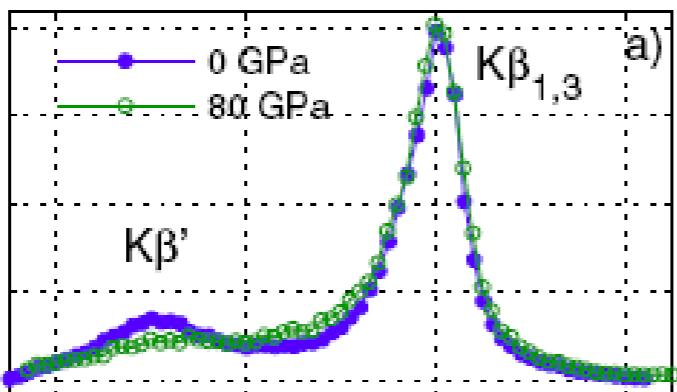
# Materials



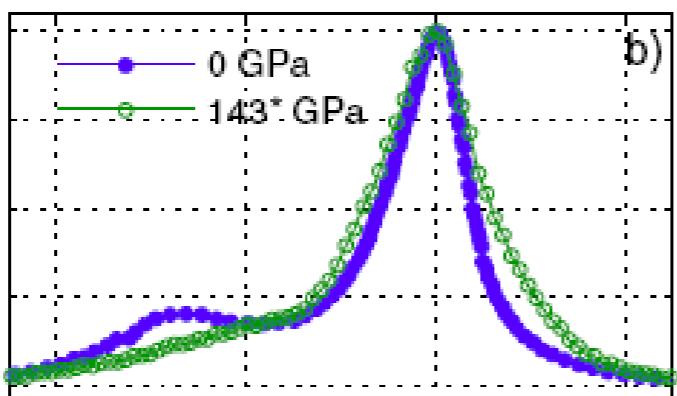
# Models



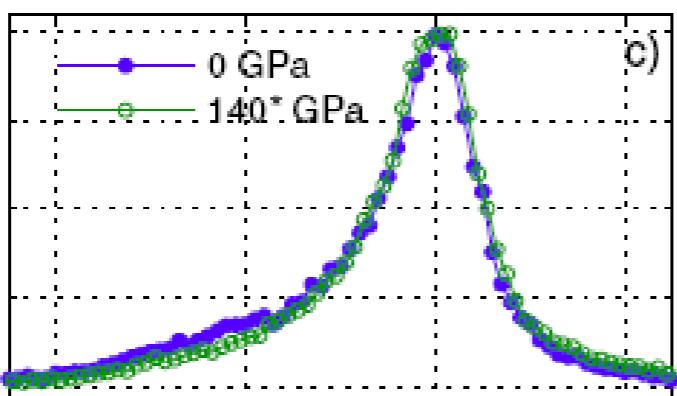
MnO



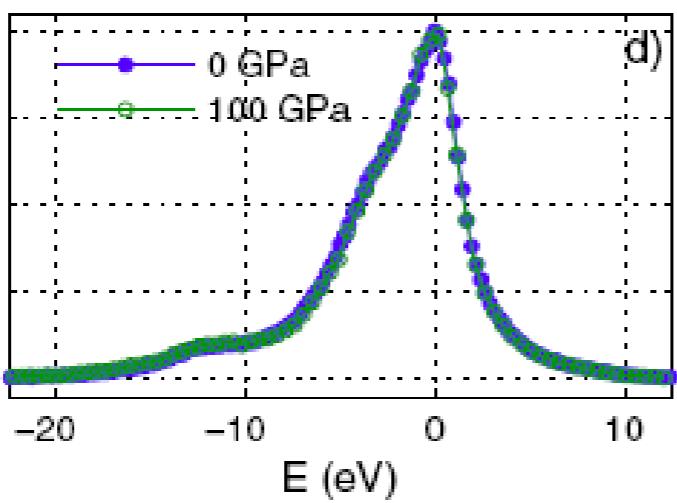
FeO



CoO

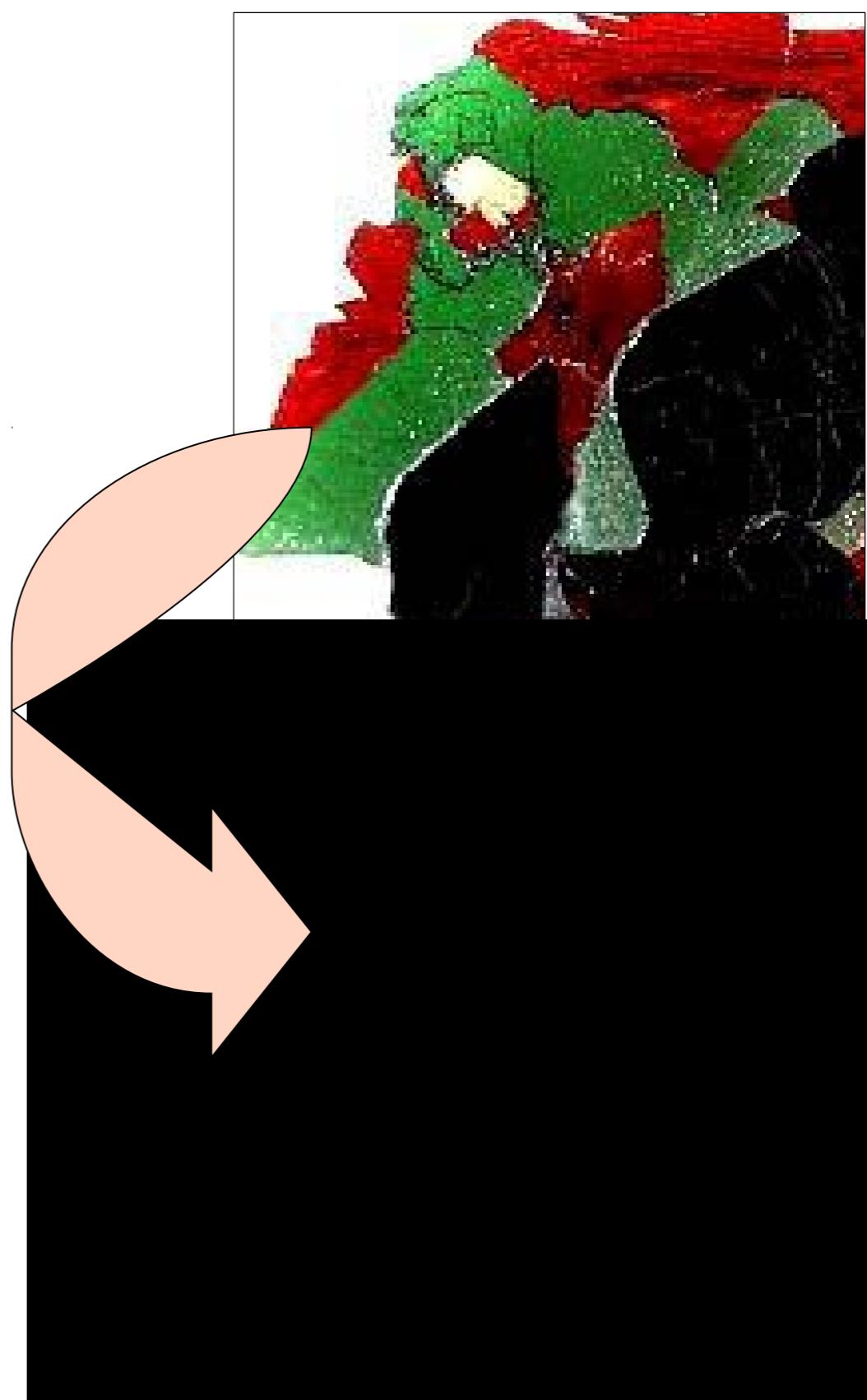


NiO

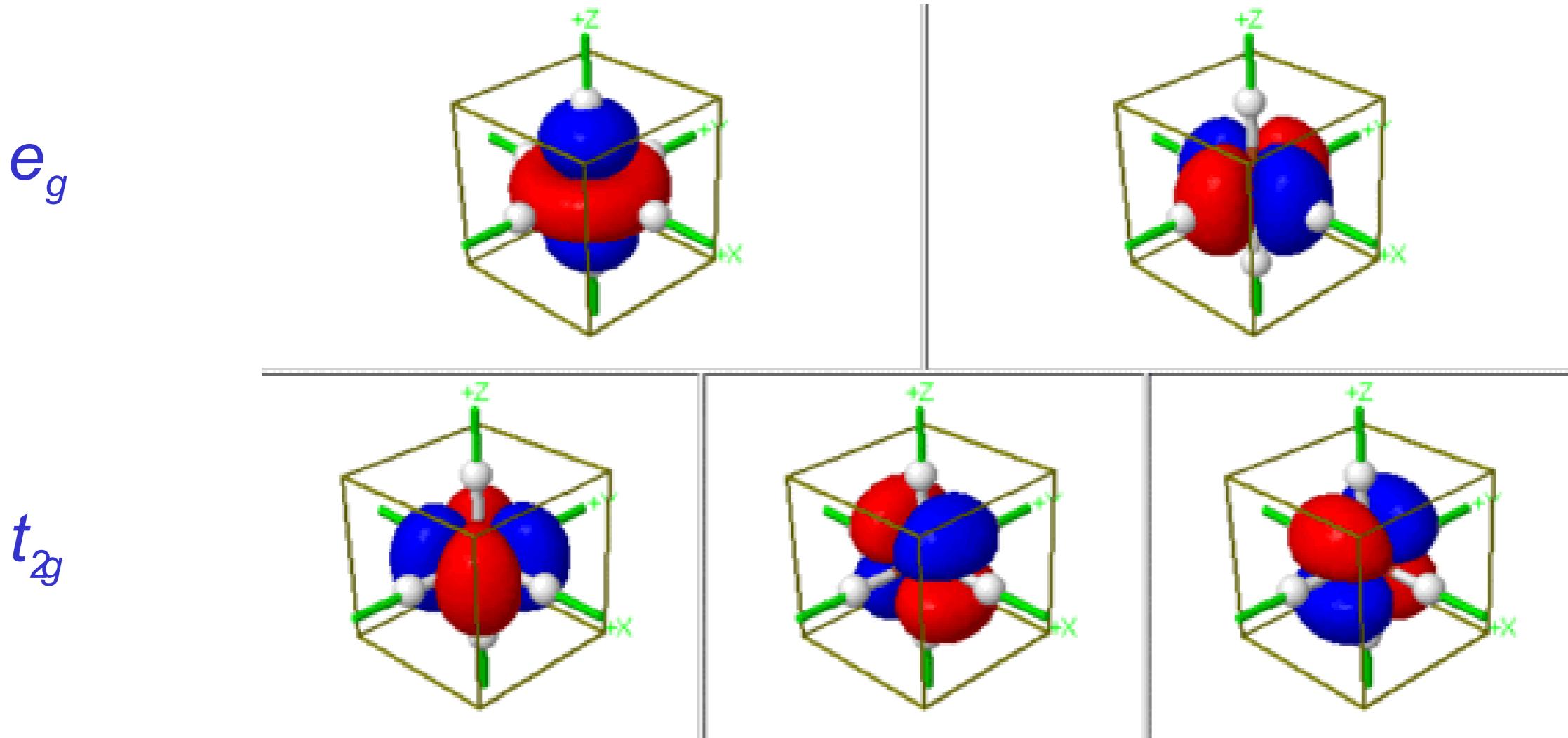


Pressure

MnO



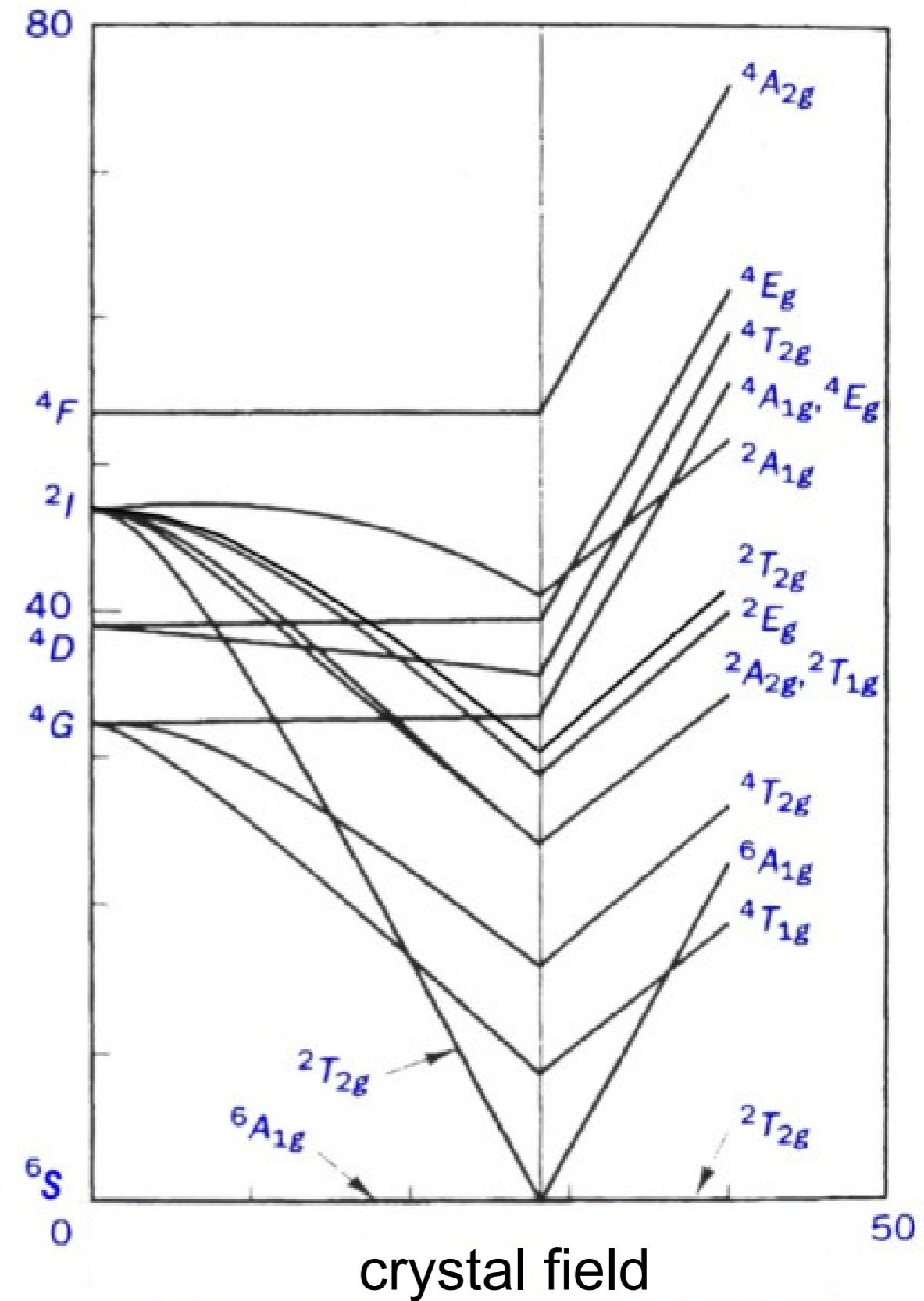
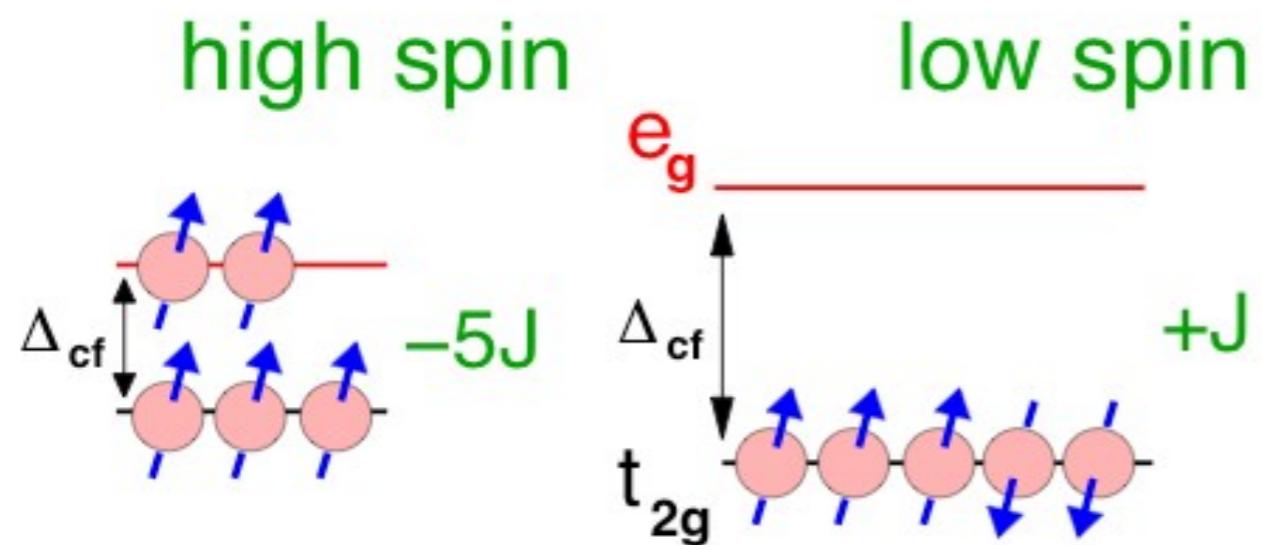
# *d*-electron in octahedral environment



Crystal-field splitting:  
electrostatic forces  
hybridization (band repulsion)

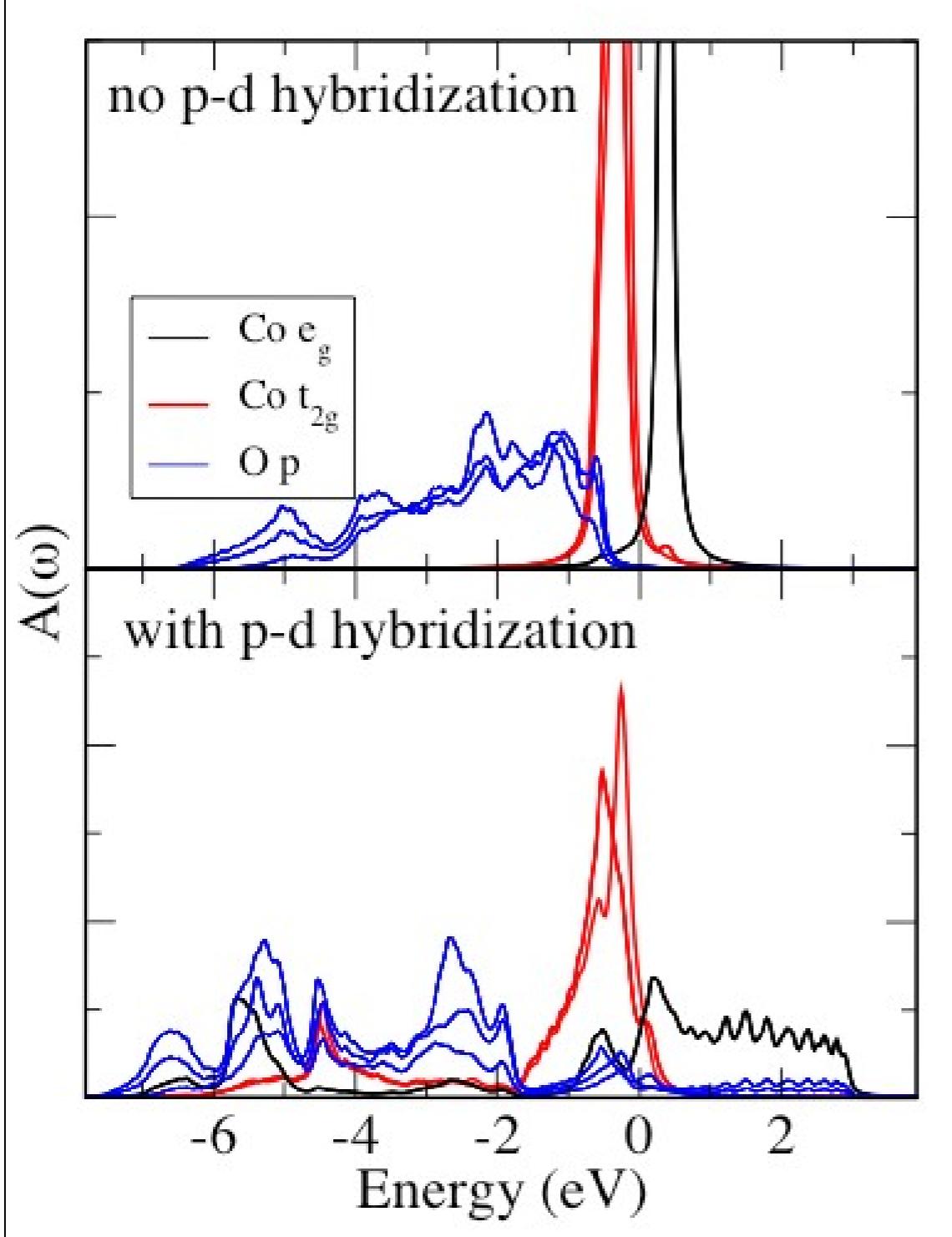
# $d$ -multiplets in octahedral field

Tanabe-Sugano diagram for  $d^5$



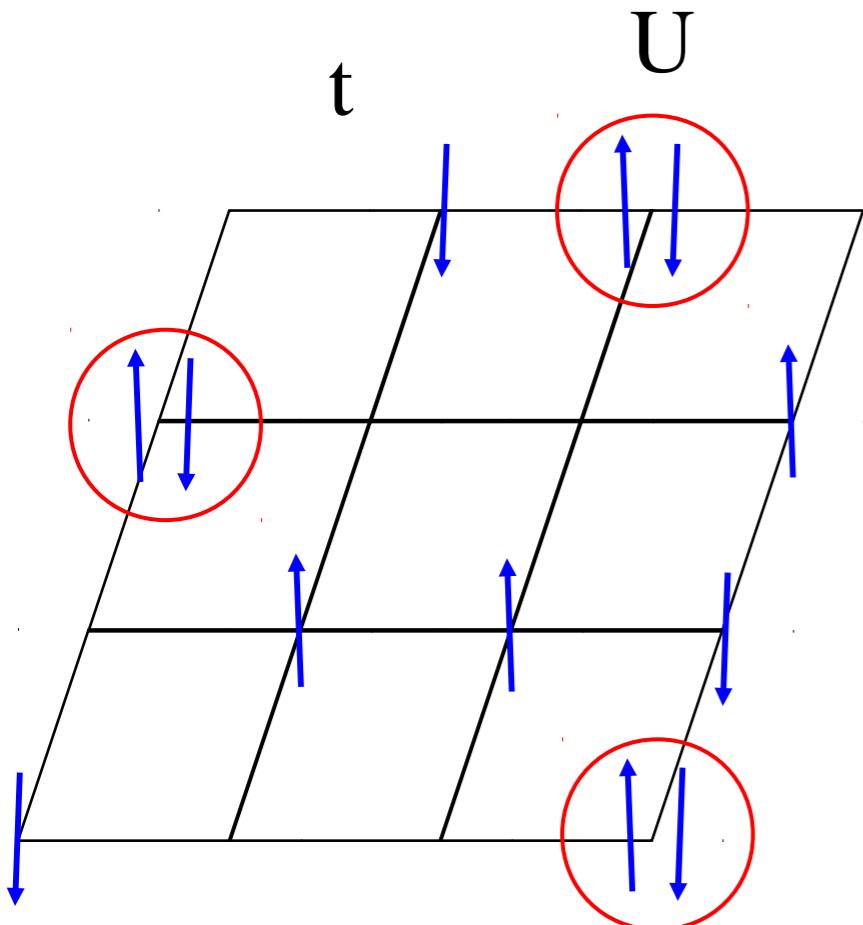
# Transition metal oxides- band structure

LDA bands for  $\text{LaCoO}_3$



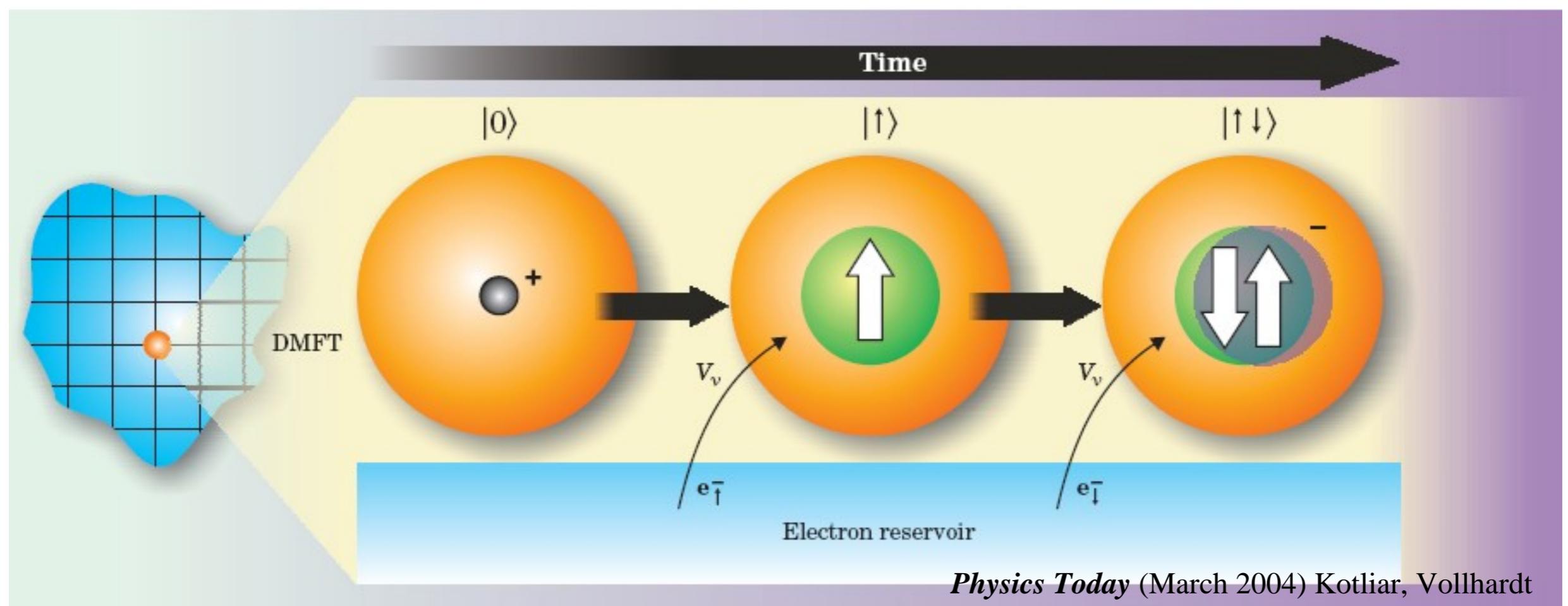
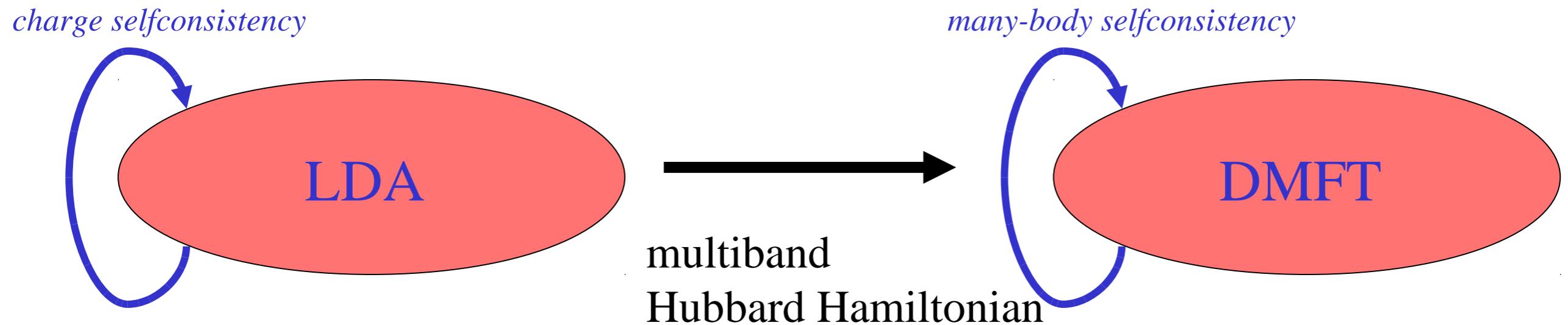
- hopping from TM ions mostly through oxygen
- $p-e_g$  hybridization  $\Rightarrow$  broad  $e_g$  band CF splitting
- relative position of  $d$  and  $p$  bands not necessarily correct

# Electron correlations and Hubbard model



- competition between kinetic and interaction energy: itinerancy vs localization
- localization -> large (quasi)degeneracy-> temperature (entropy) becomes important parameter
- emergence - new (non-fermionic) degrees of freedom appear, e.g. local spin, orbital-pseudospin -> possibility of new ordered states
- fluctuations of the emergent degrees of freedom - both quantum mechanical and statistical

# Dynamical Mean-Field Theory (LDA+DMFT)

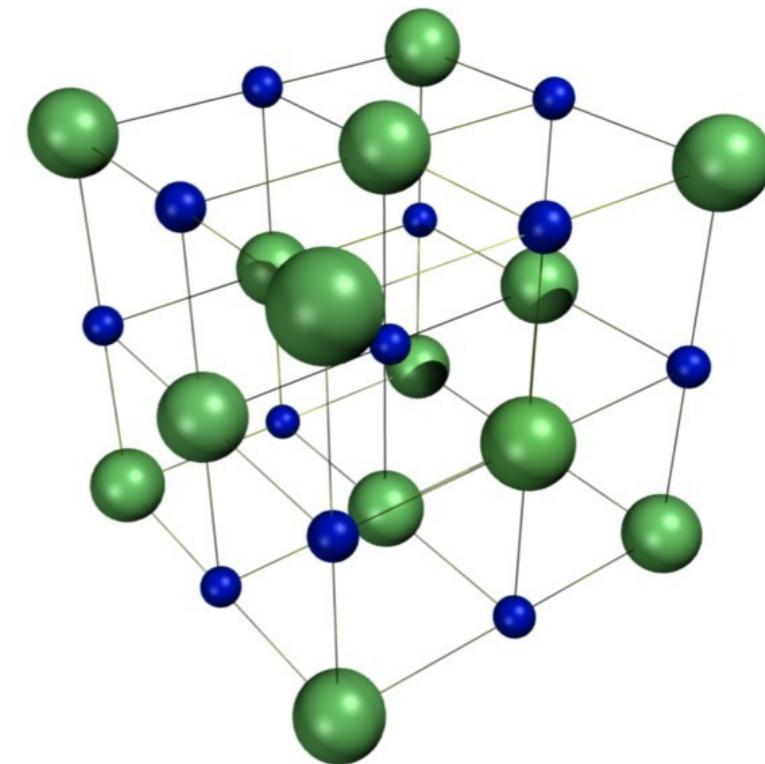
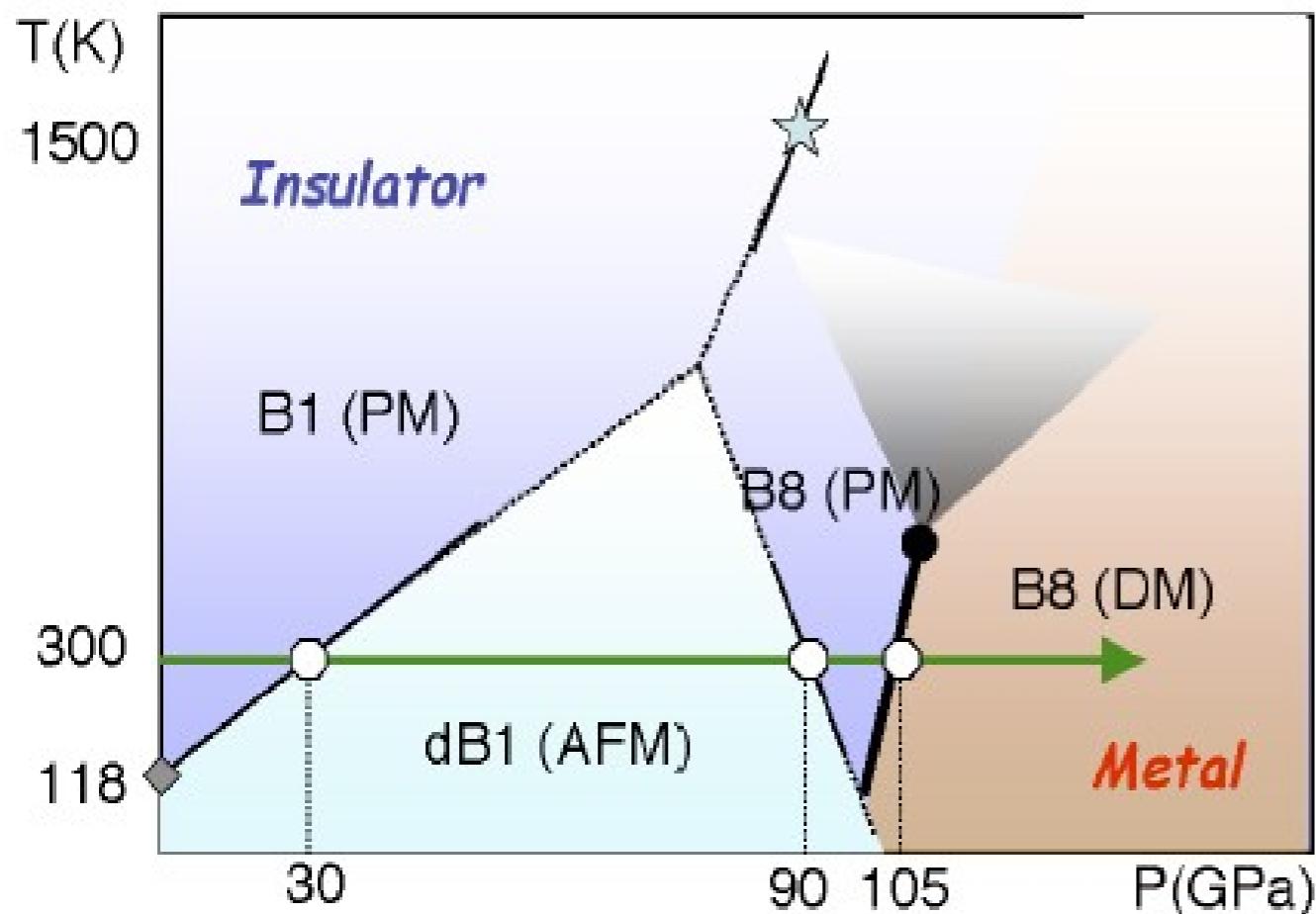


*Physics Today* (March 2004) Kotliar, Vollhardt

# MnO experimental summary

$\text{Mn}^{2+} \text{O}^2 \Rightarrow \text{d}^5$  local configuration

Conceptual phase diagram of MnO



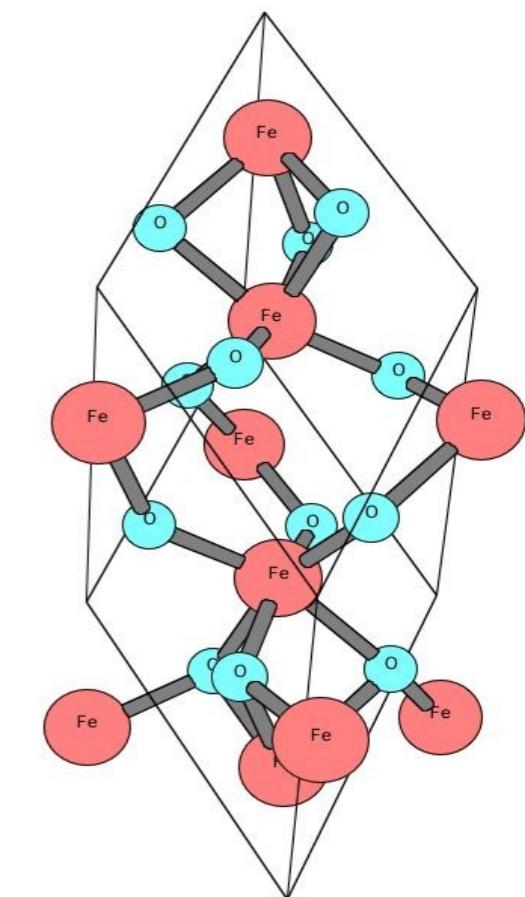
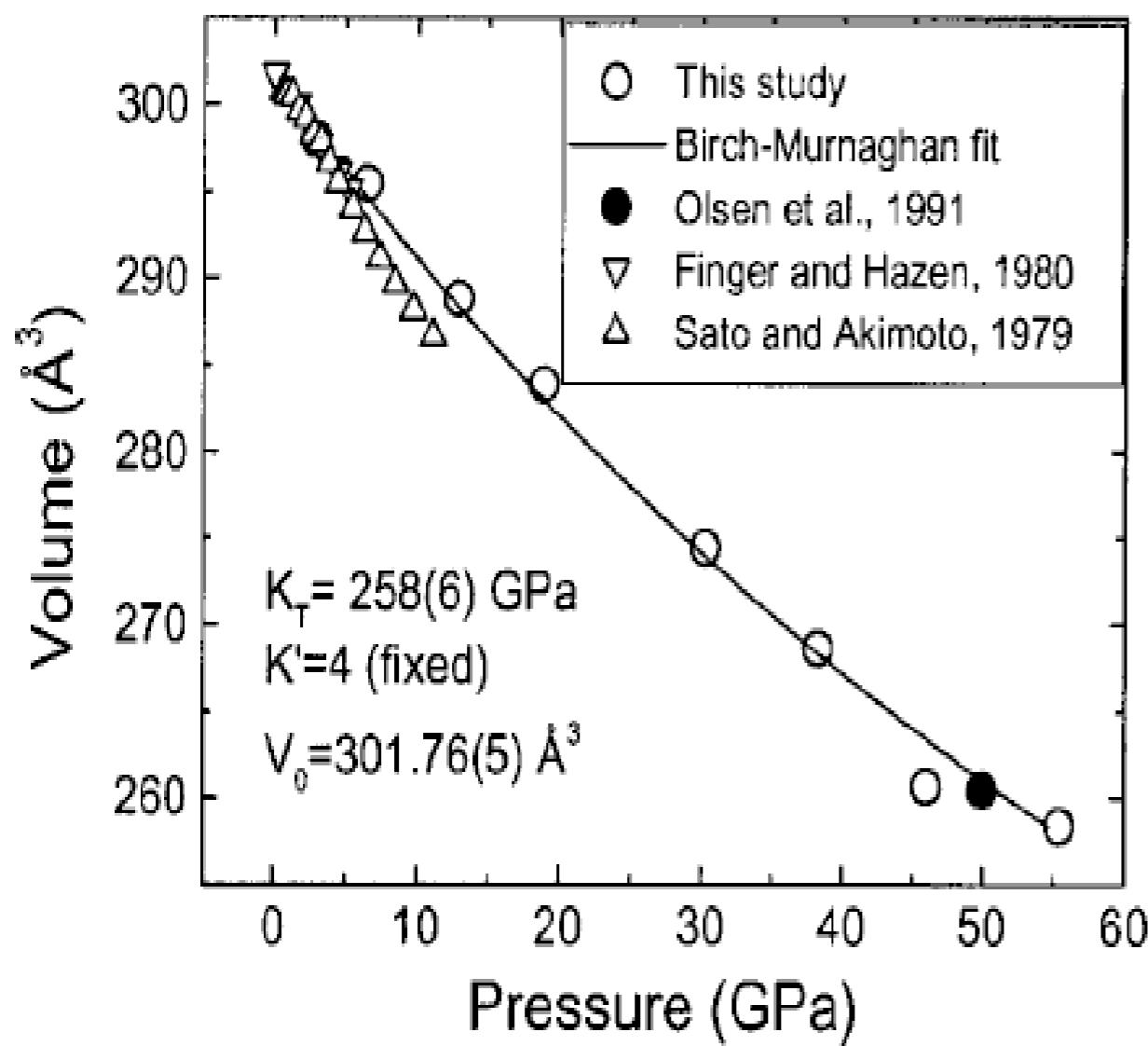
- moment collapse
- insulator -> metal transition
- volume collapse
- structural transition

# $\text{Fe}_2\text{O}_3$ experimental summary

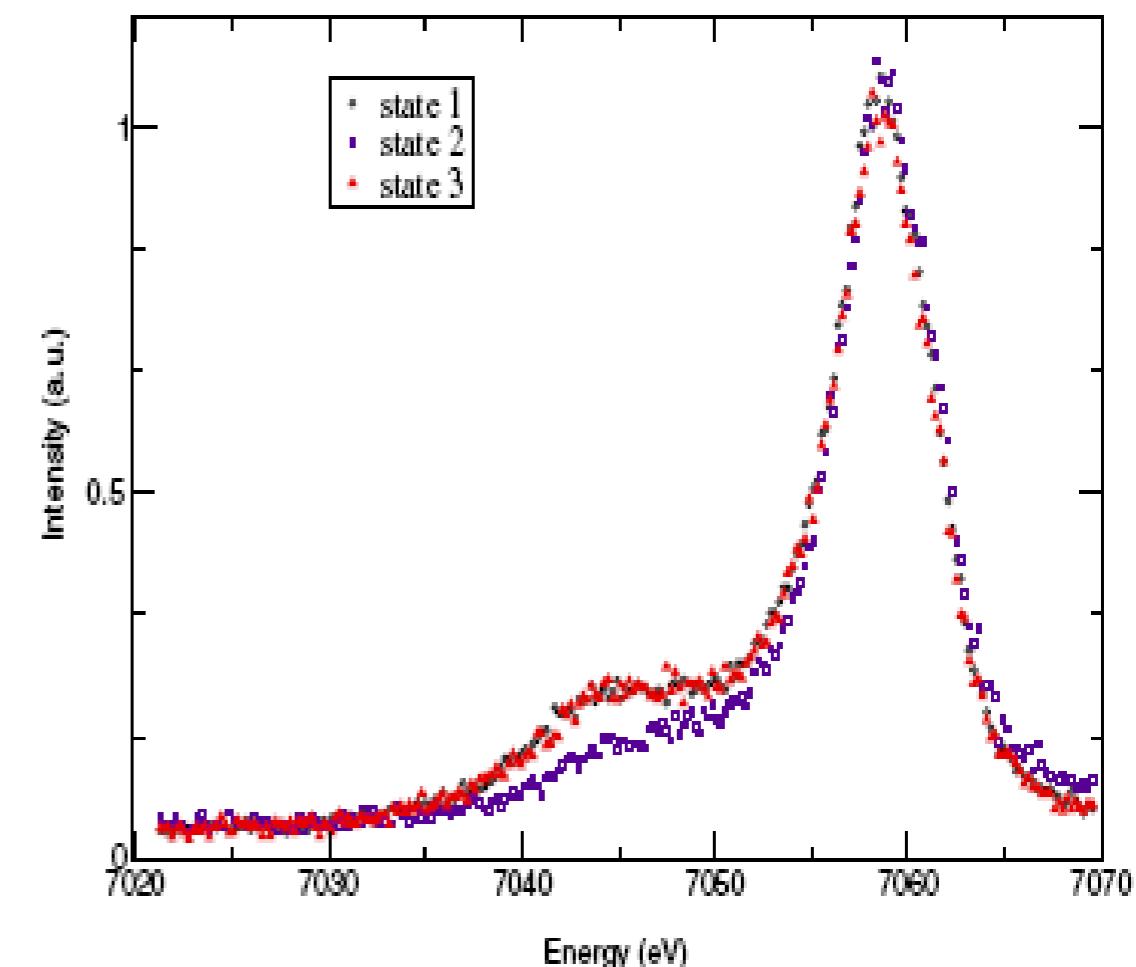
$\text{Fe}_2^{3+} \text{O}_3^{2-} \Rightarrow \text{d}^5$  local configuration

Fe in octahedral coordination

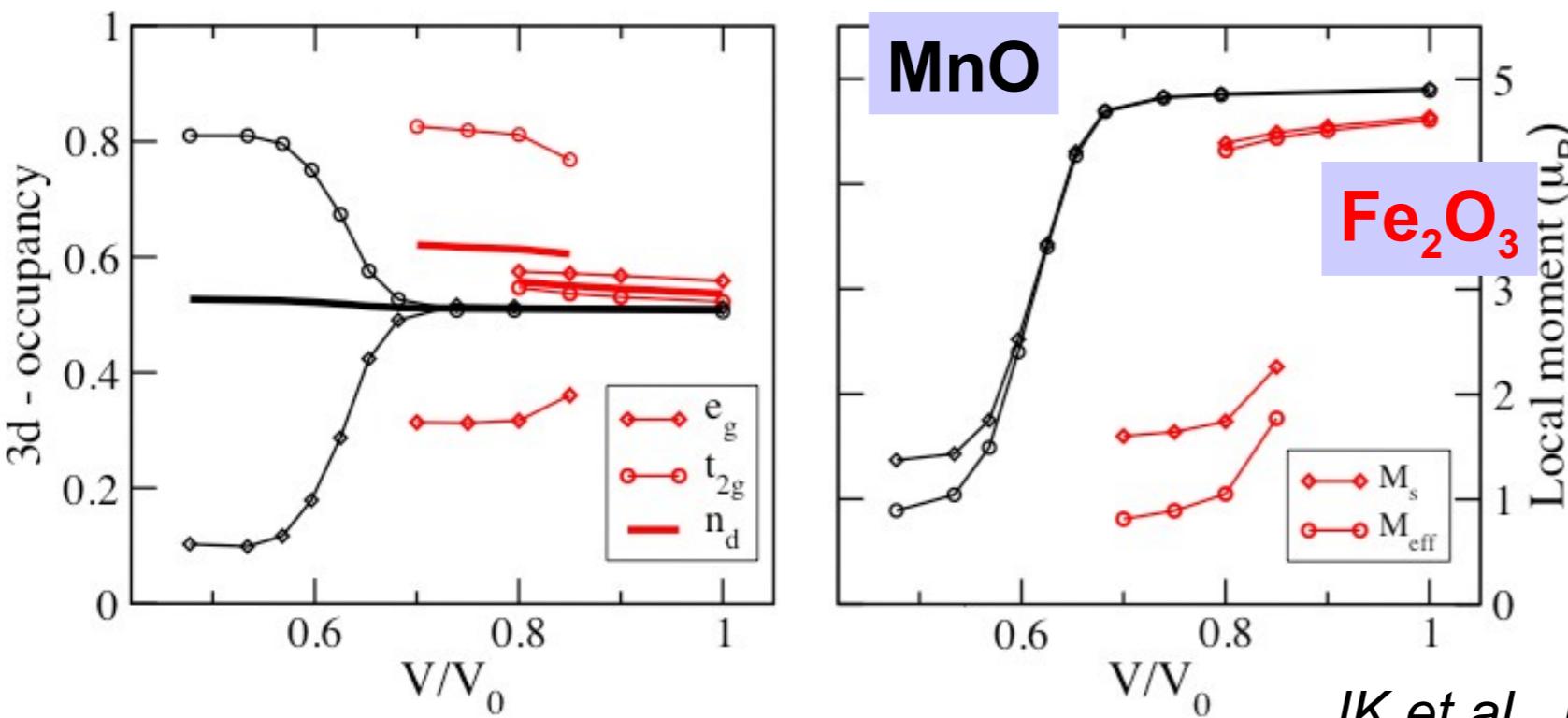
Rosenberg et al., Phys. Rev. B 65, 064112 (2002)



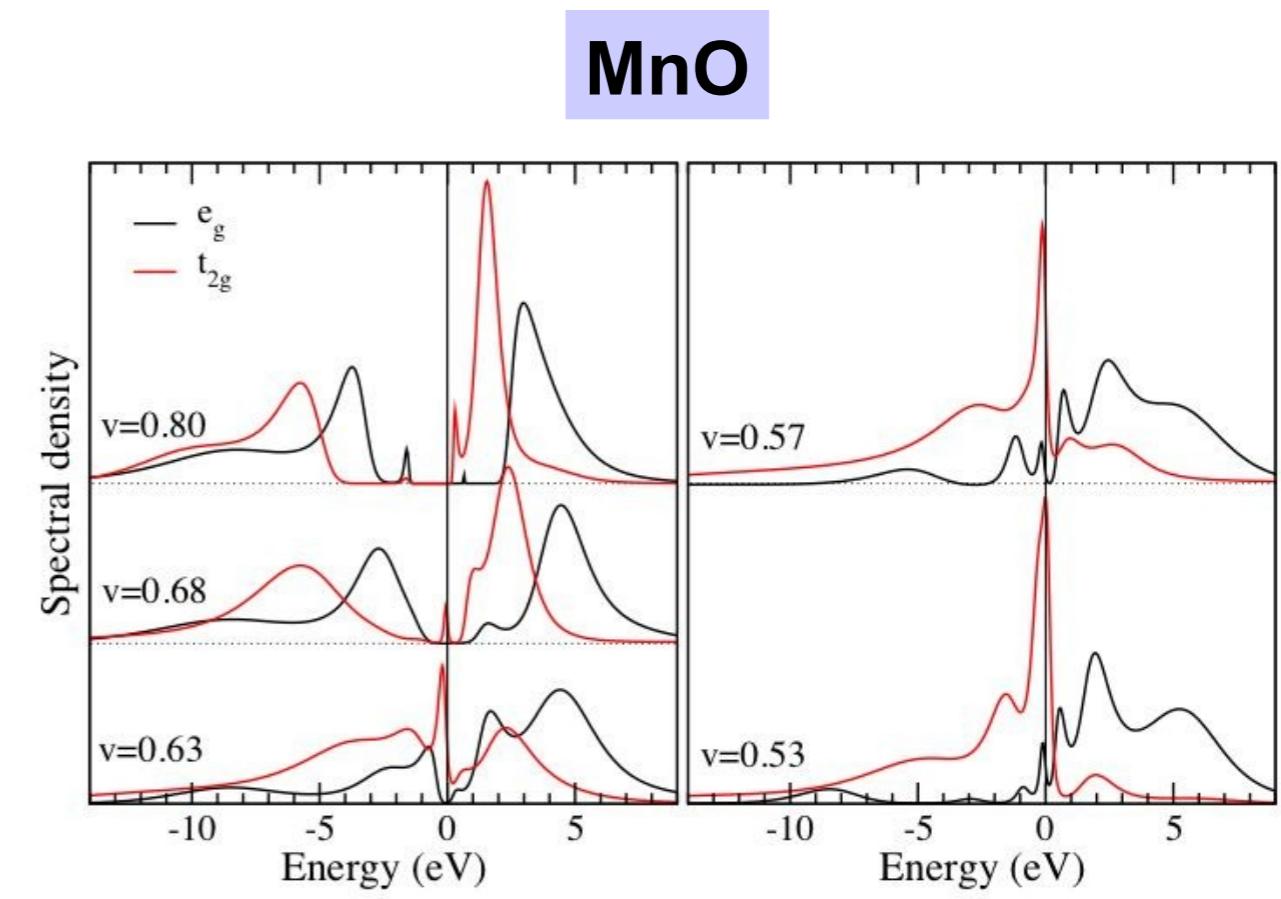
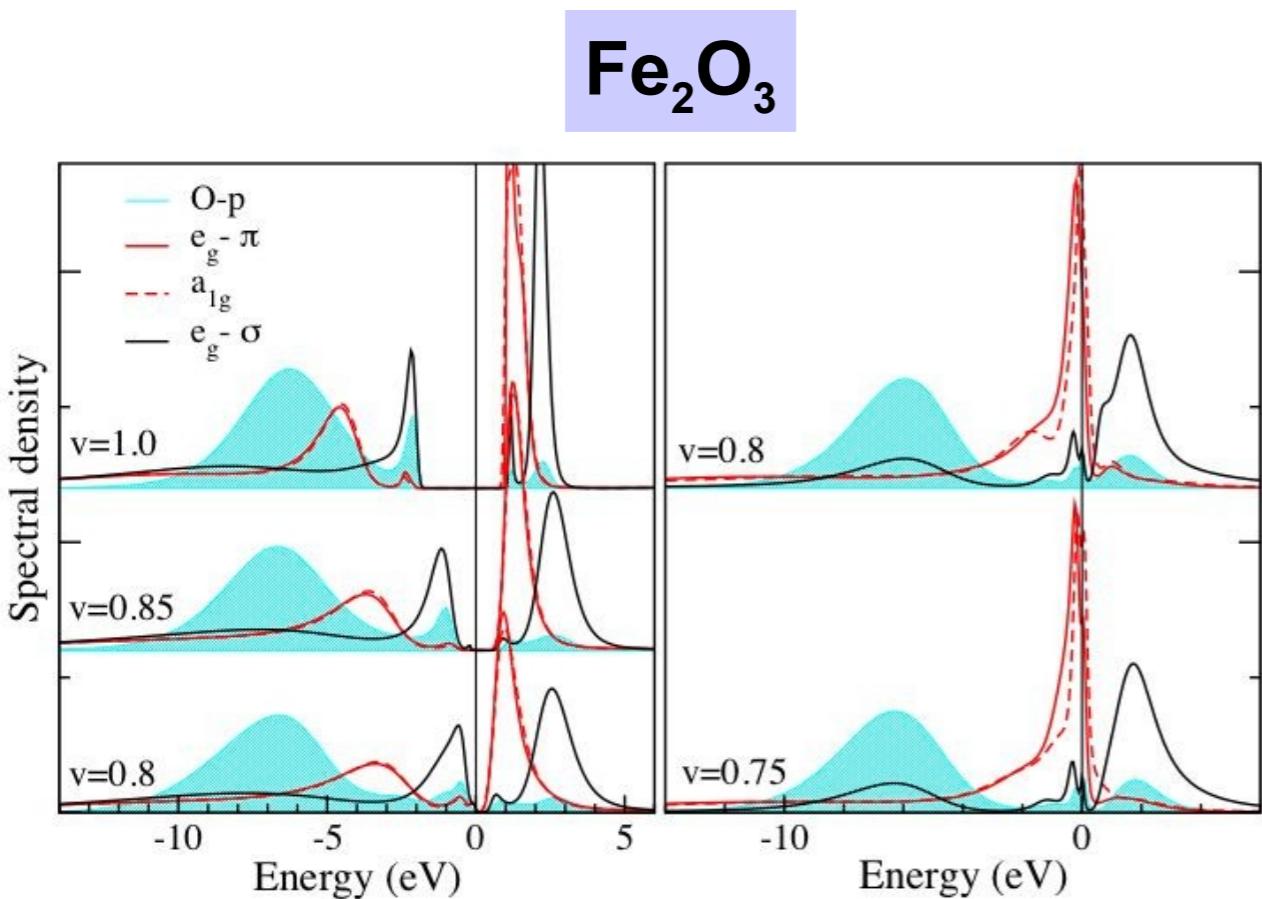
Badro et al., Phys. Rev. Lett. 89, 205504 (2002)



# Pressure driven spin state transition

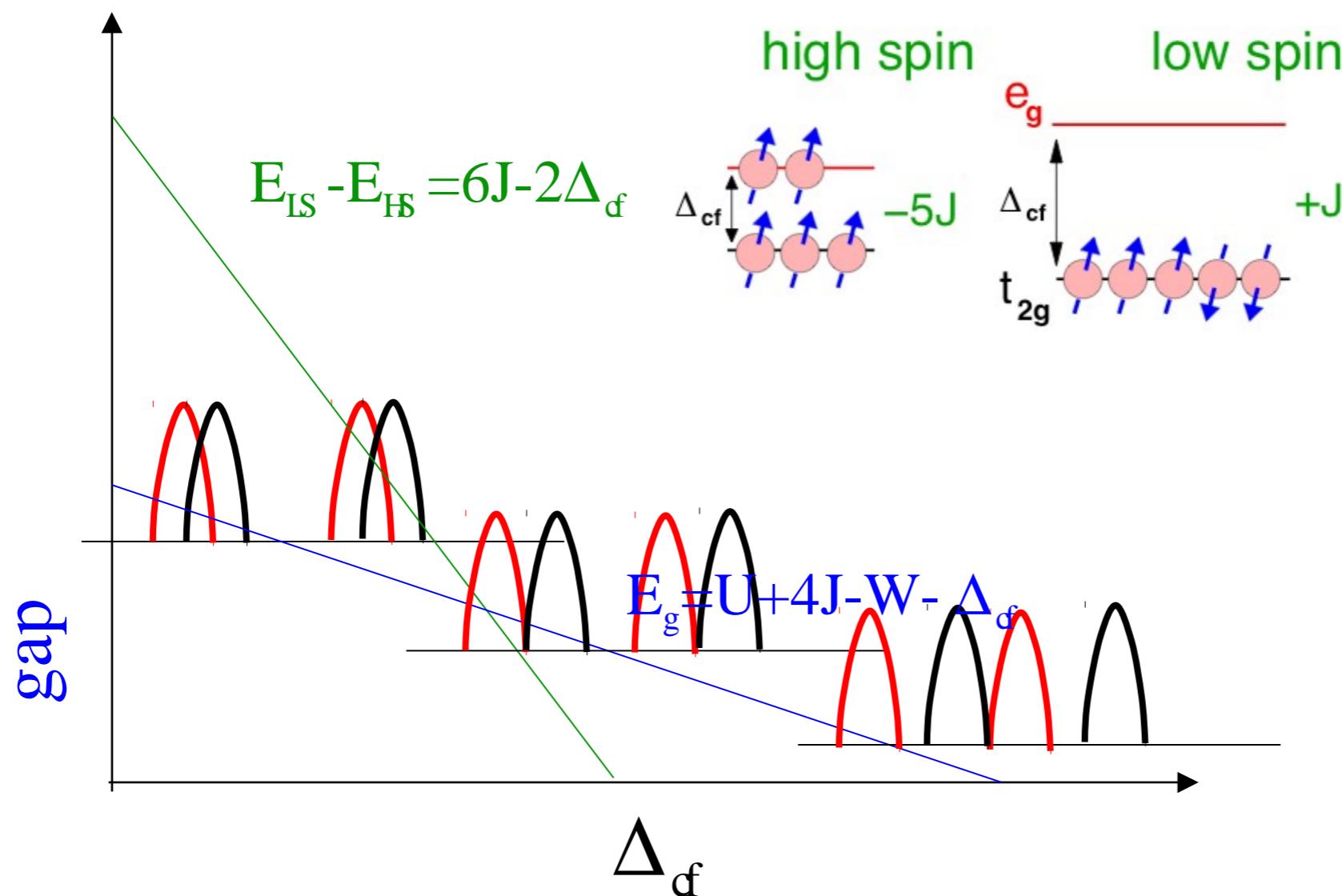


*JK et al., Nature Materials 7, 198 (2008)*  
*JK et al., Phys. Rev. Lett. 102, 146402 (2009)*



# Pressure induced metallization

Gap closing vs local spin state transition



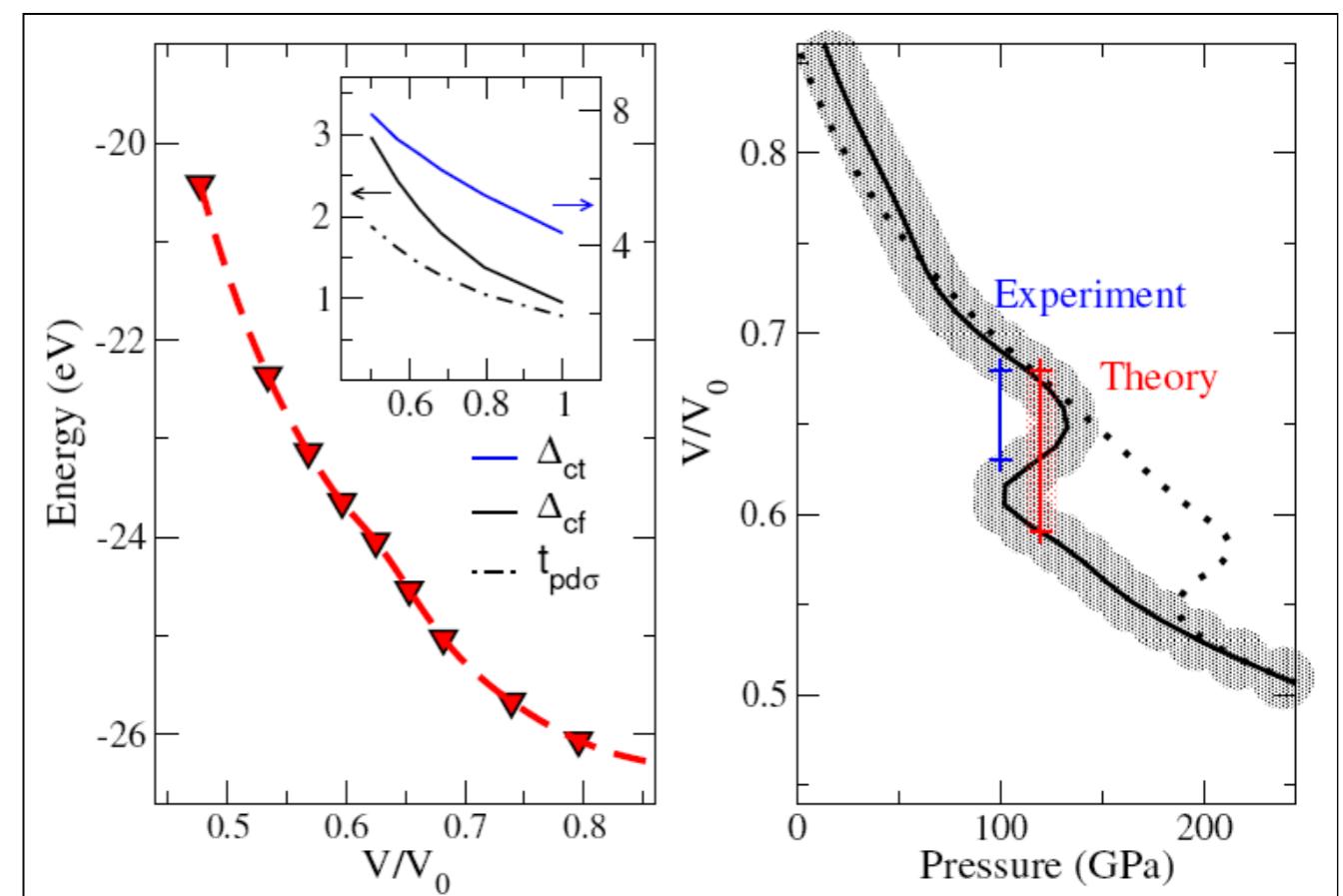
# Pressure induced transitions - summary

two scenarios:

- **local state transition** - atomic physics dominates  
metallicity is slave to atomic constraints
- **gap closing** - hopping plays active role in the transition

Energy scale:  
 $\sim 1 \text{ eV/atom}$

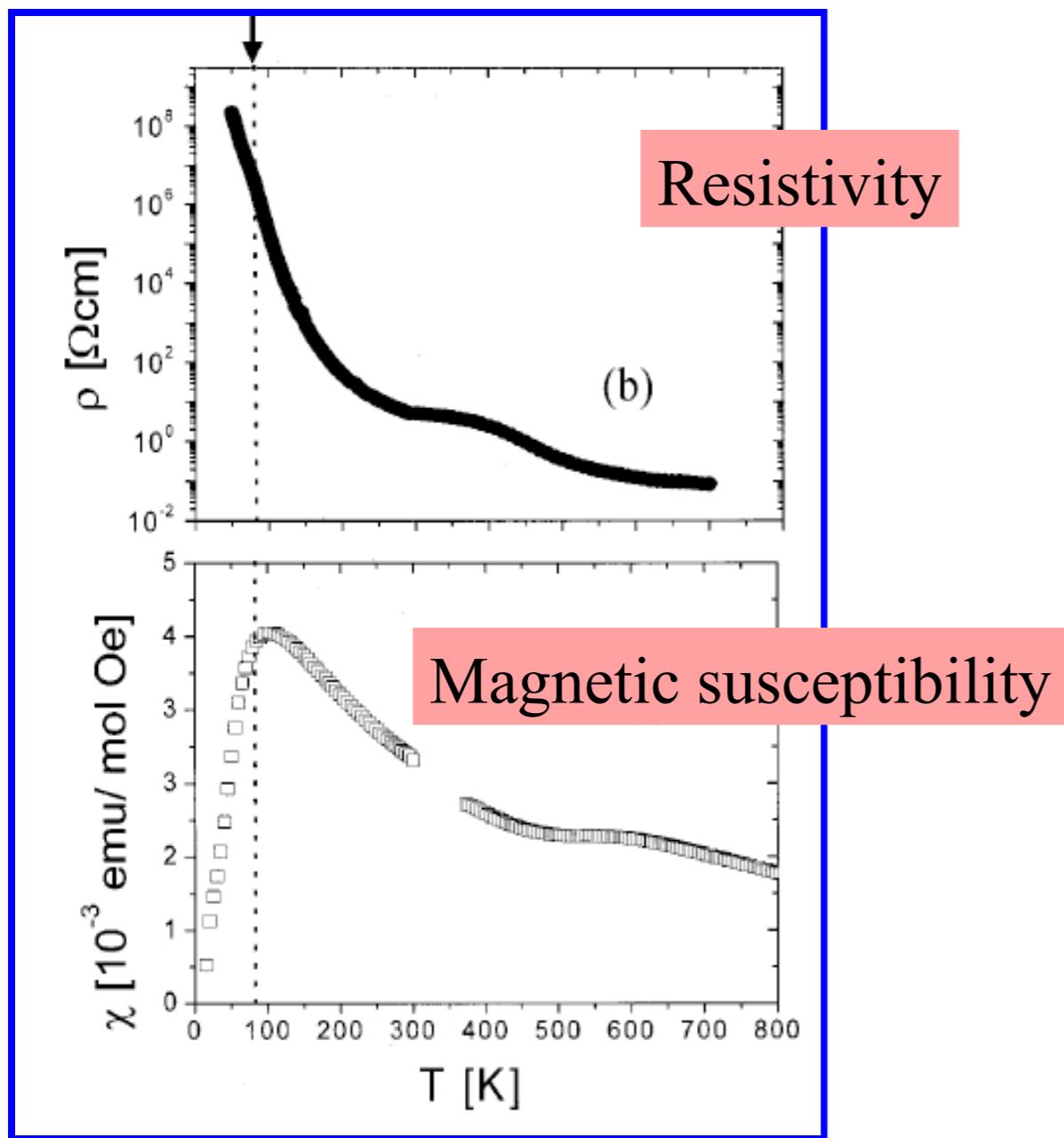
Pressure scale:  
10-100 GPa  
( $\sim 1 \text{ GPa width}$ )



What happens right at the transition?

# What happens right at the transition?

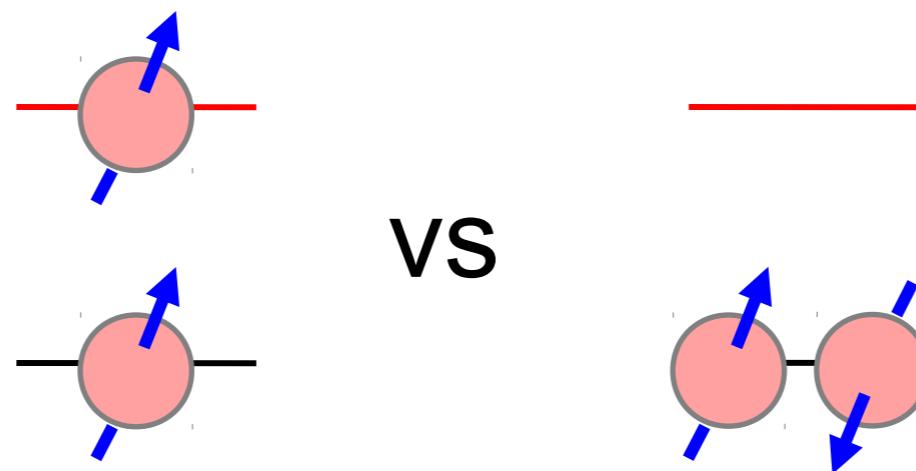
$\text{LaCoO}_3$  - nature did the fine tuning job for us !



- $d^6$  state for  $\text{Co}^{3+}$  valence
- $S=0$  LS vs  $S=2$  or  $1$  ? HS
- $E_{\text{LS}} < E_{\text{HS}}$  ,  $E_{\text{HS}} - E_{\text{LS}} \sim kT$

# Two-band Hubbard model

$$\begin{aligned} H = & \sum_{i,\sigma} ((\Delta - \mu) n_{i,\sigma}^a - \mu n_{i,\sigma}^b) + \sum_{\langle ij \rangle, \sigma} (t_{aa} a_{i,\sigma}^\dagger a_{j,\sigma} + t_{bb} b_{i,\sigma}^\dagger b_{j,\sigma}) \\ & + U \sum_i (n_{i,\uparrow}^a n_{i,\downarrow}^a + n_{i,\uparrow}^b n_{i,\downarrow}^b) + (U - 2J) \sum_{i,\sigma} n_{i,\sigma}^a n_{i,-\sigma}^b \\ & + (U - 3J) \sum_{i,\sigma} n_{i,\sigma}^a n_{i,\sigma}^b \end{aligned}$$

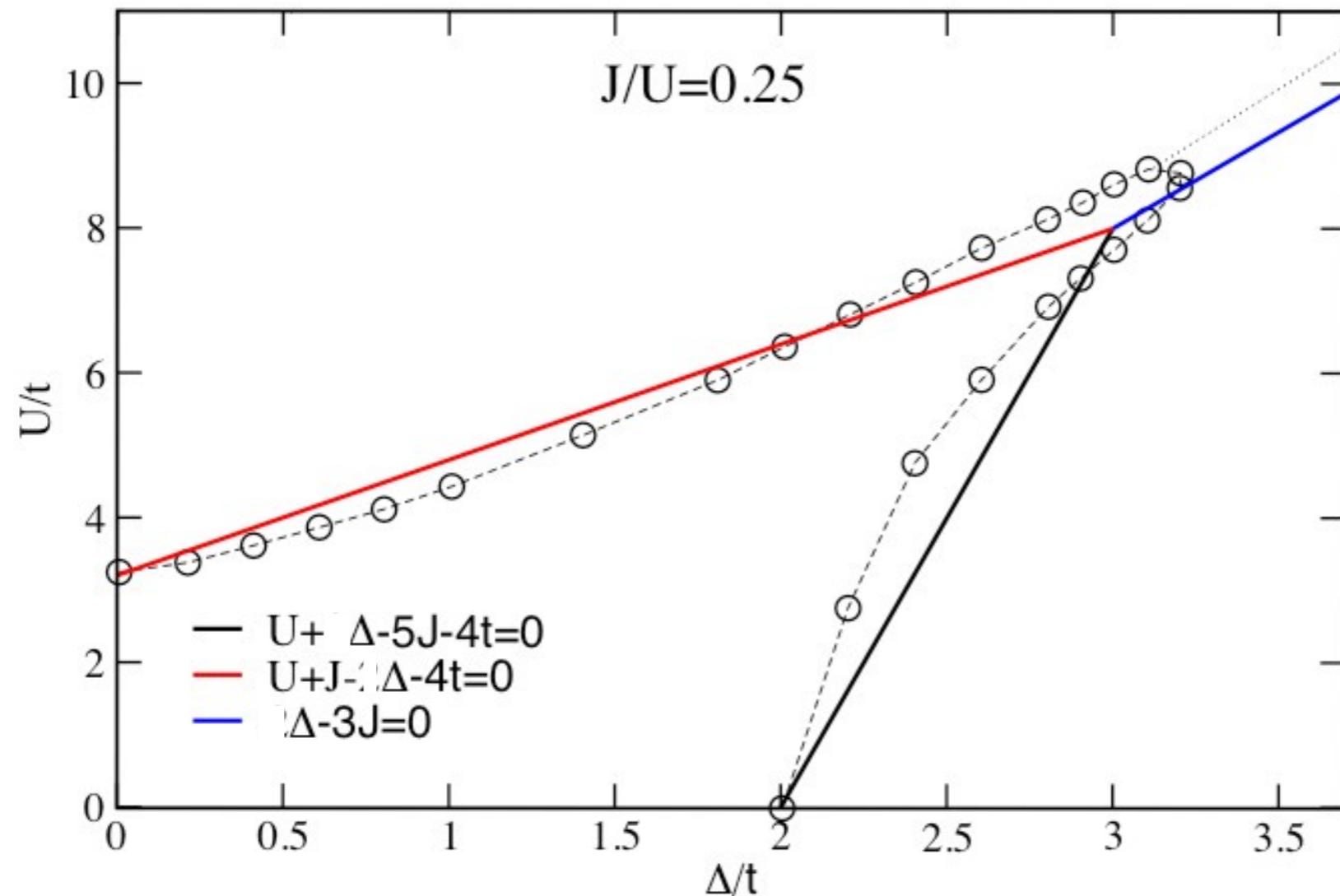


# U- $\Delta$ phase diagram

$\Delta$  - crystal field

J/U - fixed

2D - bipartite lattice (square lattice)



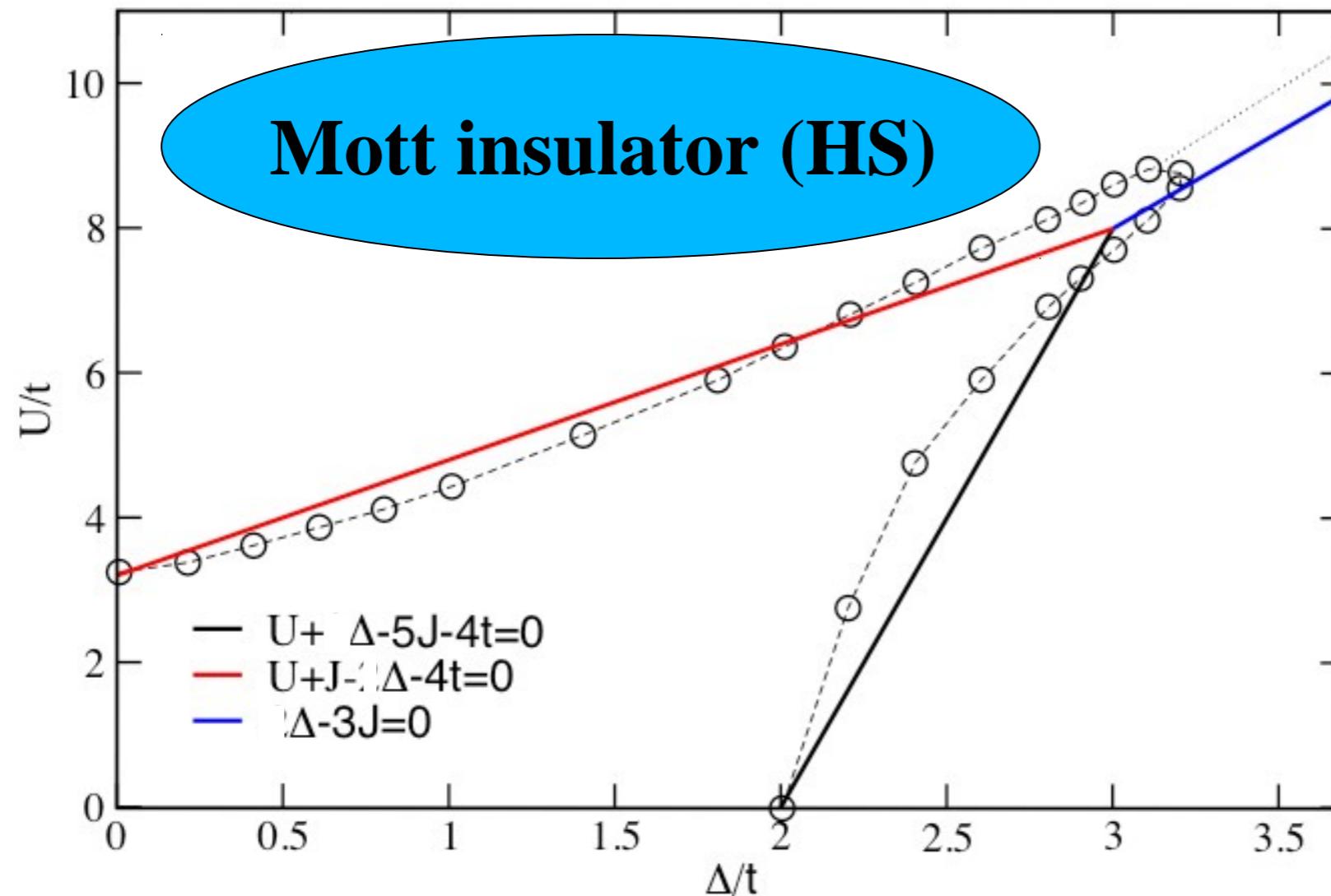
Werner & Millis, Phys. Rev. Lett. **99**, 126405 (2007)  
JK et al. Eur. Phys. J. Special Topics **180**, 5 (2009)

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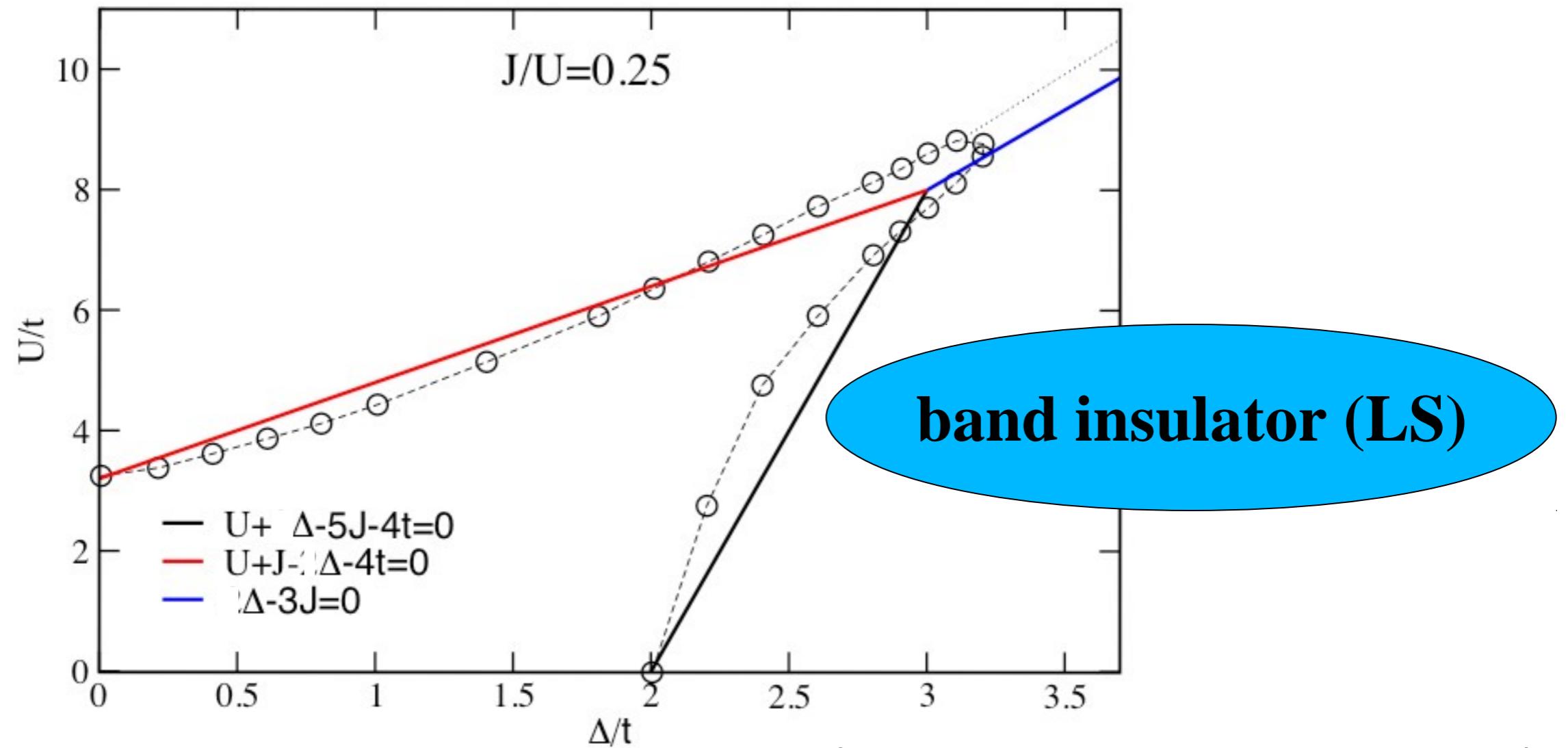
Werner & Millis, Phys. Rev. Lett. **99**, 126405 (2007)  
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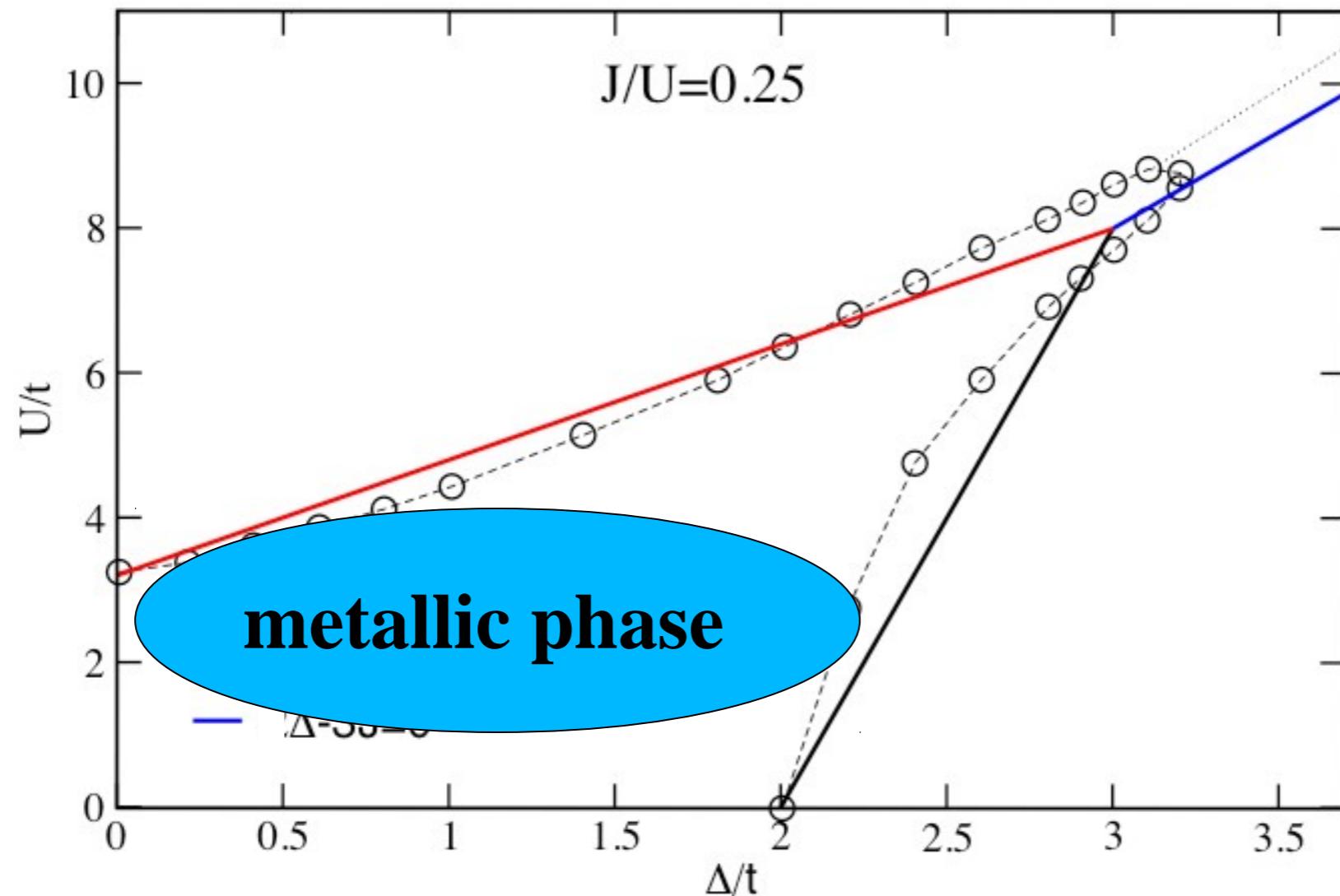
Werner & Millis, Phys. Rev. Lett. **99**, 126405 (2007)  
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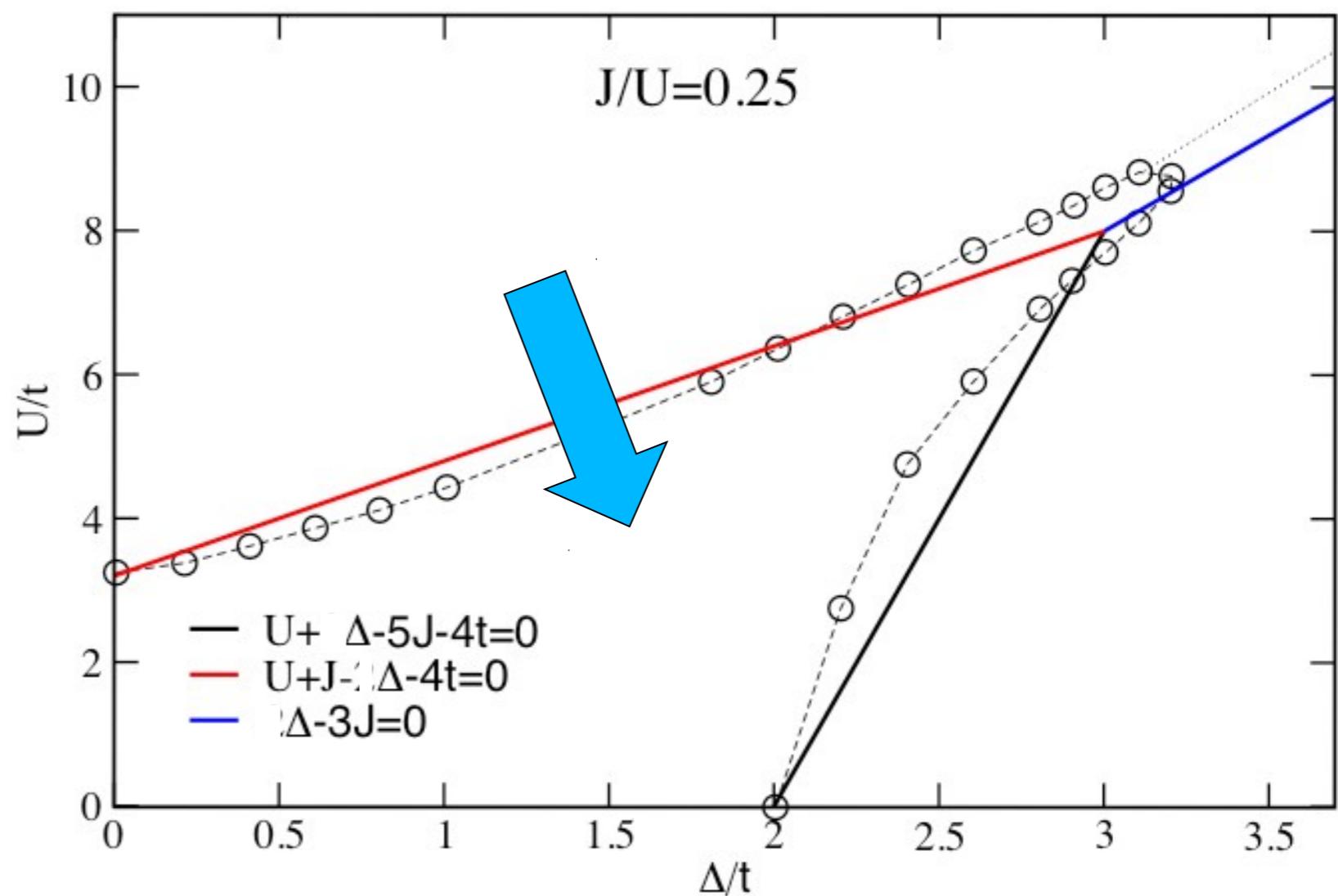
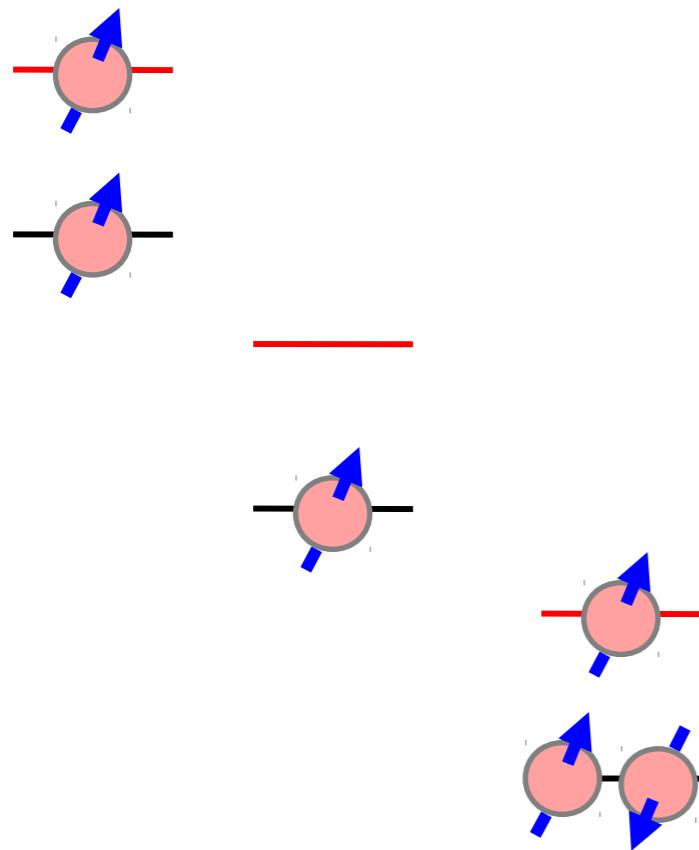


Werner & Millis, Phys. Rev. Lett. **99**, 126405 (2007)  
JK et al. Eur. Phys. J. Special Topics **180**, 5 (2009)

# Gap closing

'Mott gap = 0'

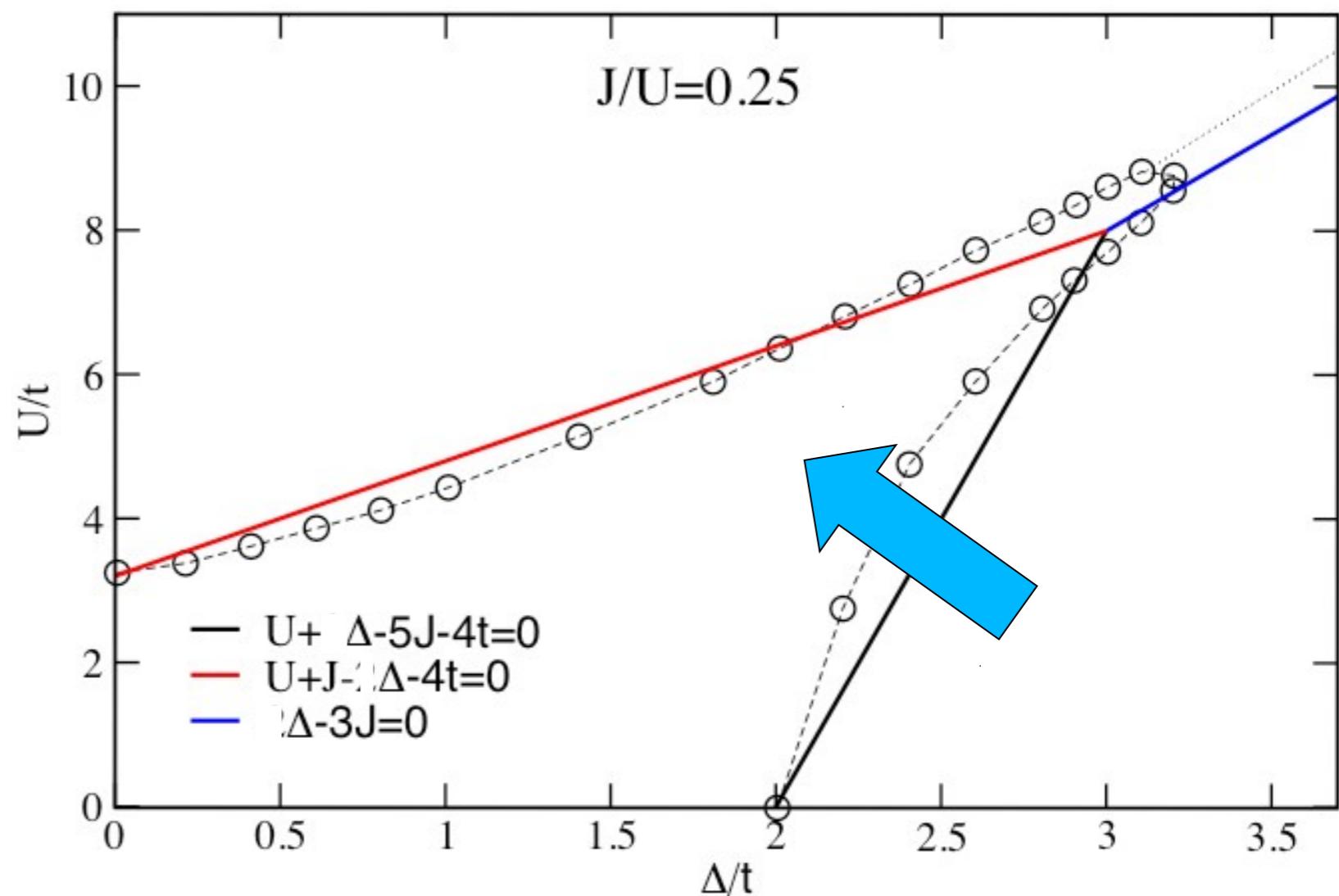
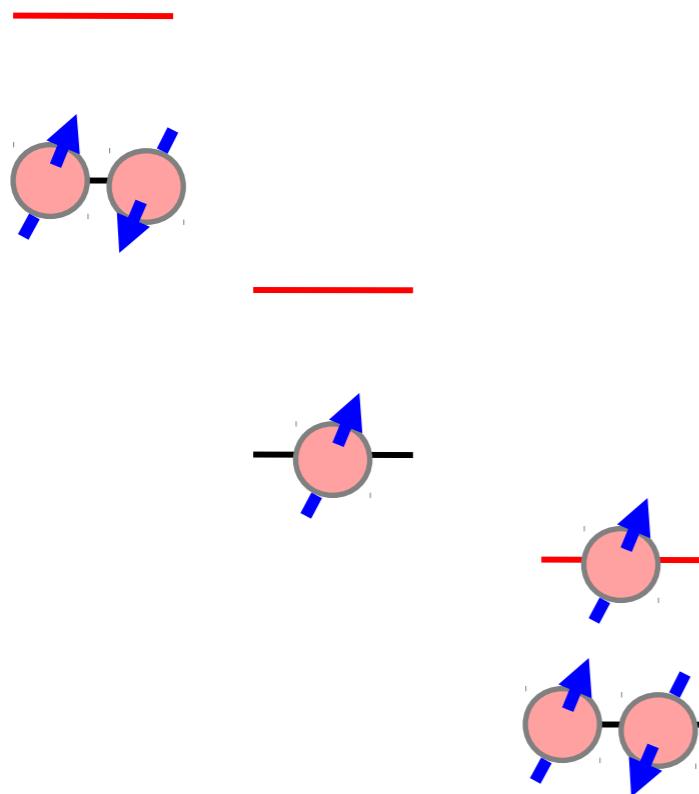
$$E_g = 2E(N) - E(N-1) - E(N+1)$$



# Band gap

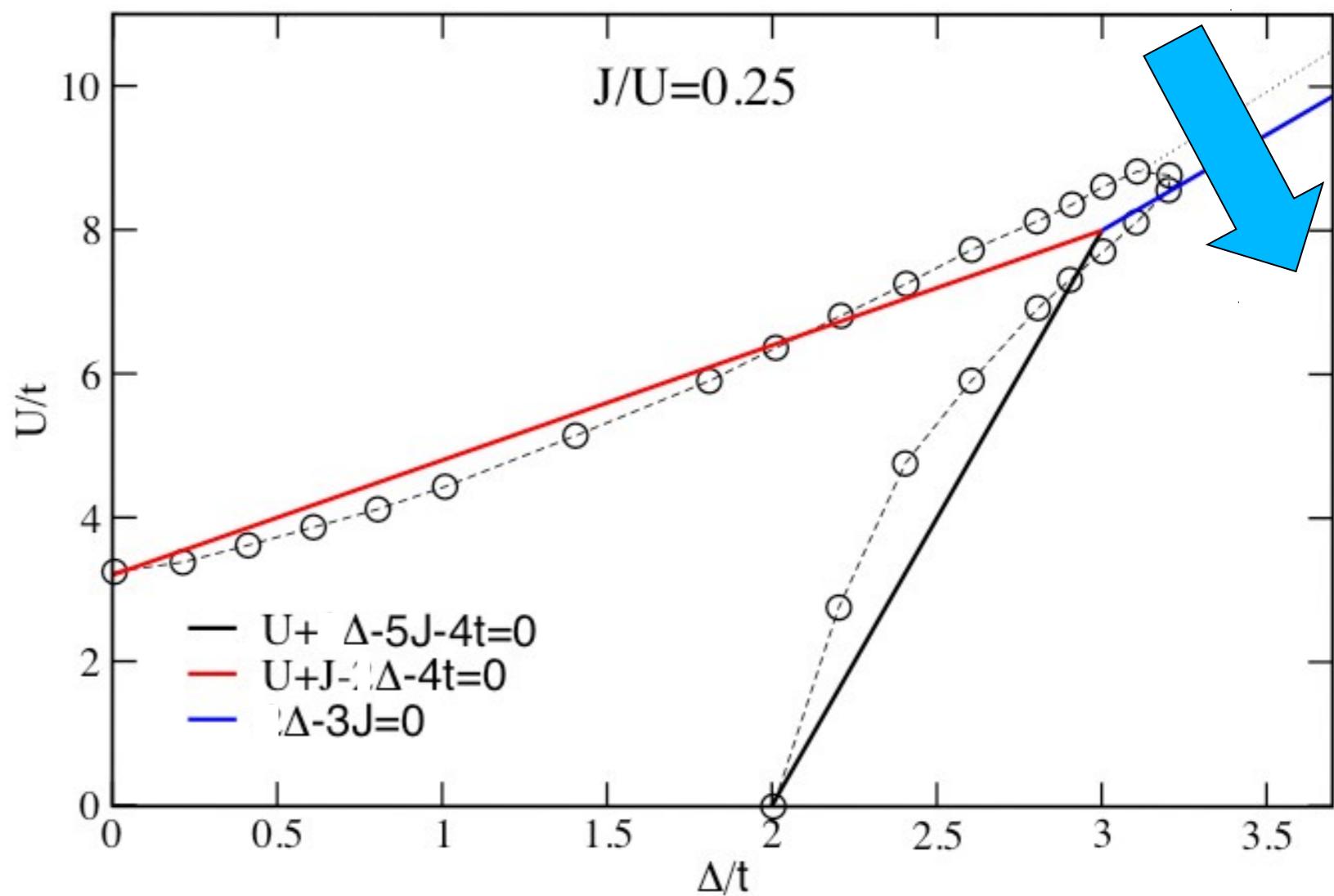
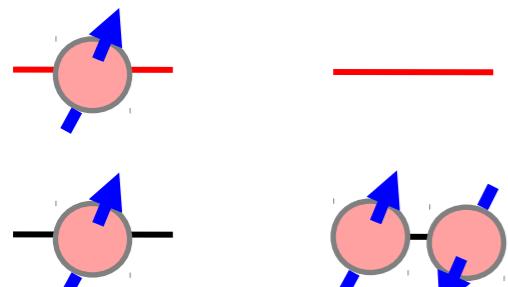
'Band gap = 0'

$$E_g = 2E(N) - E(N-1) - E(N+1)$$

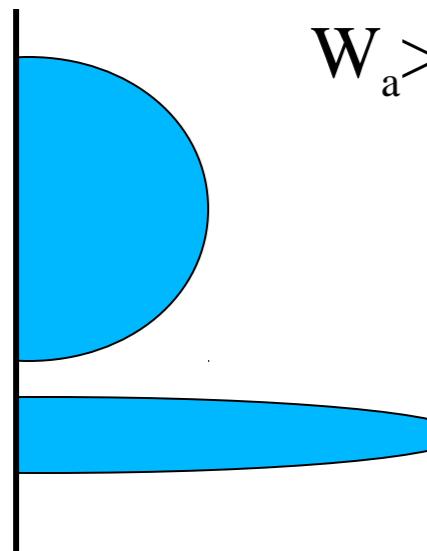


# Local state transition

' $E(HS) - E( LS) = 0$ '



# The model - stoichiometric filling=2e



*Two sublattice order allowed*

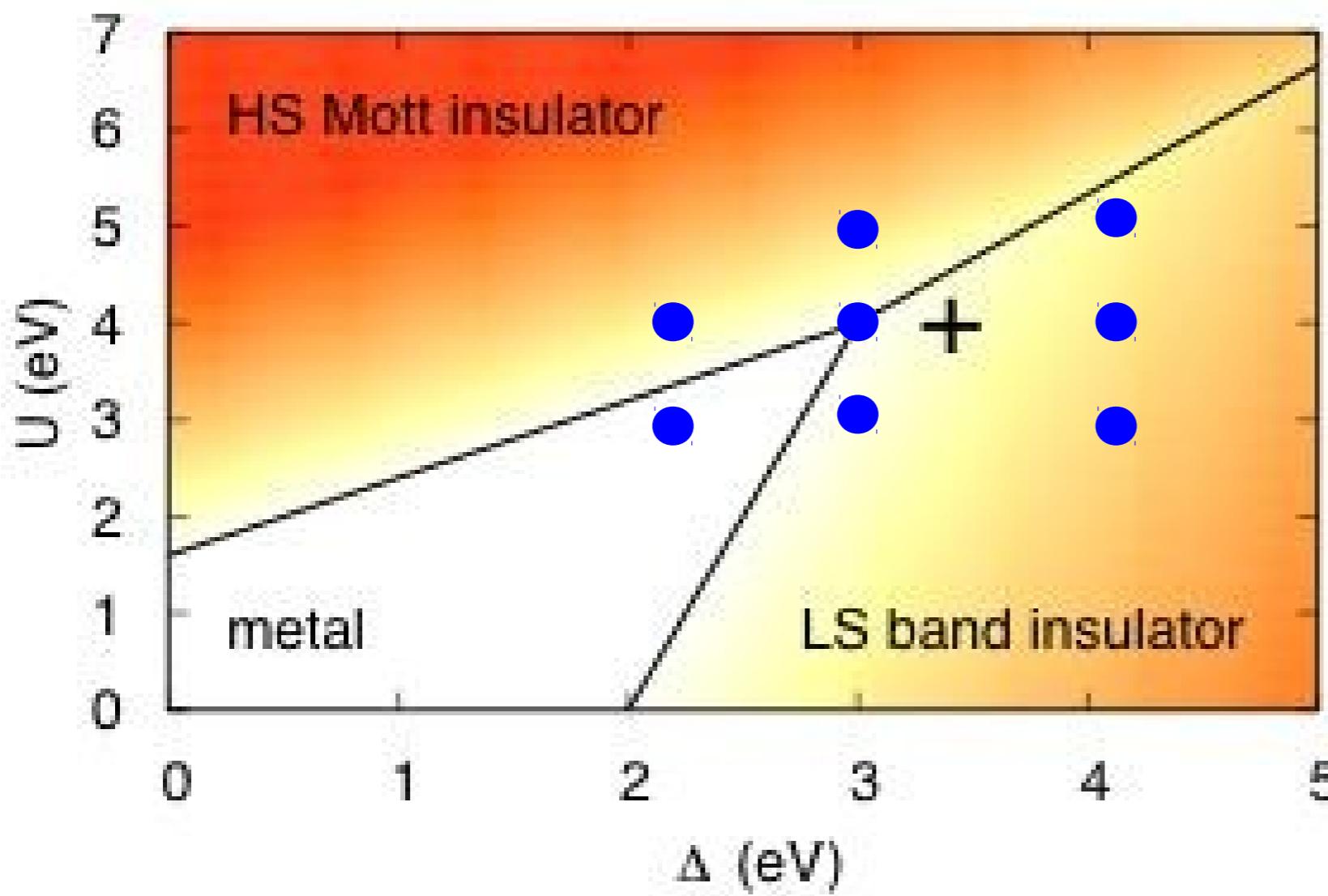
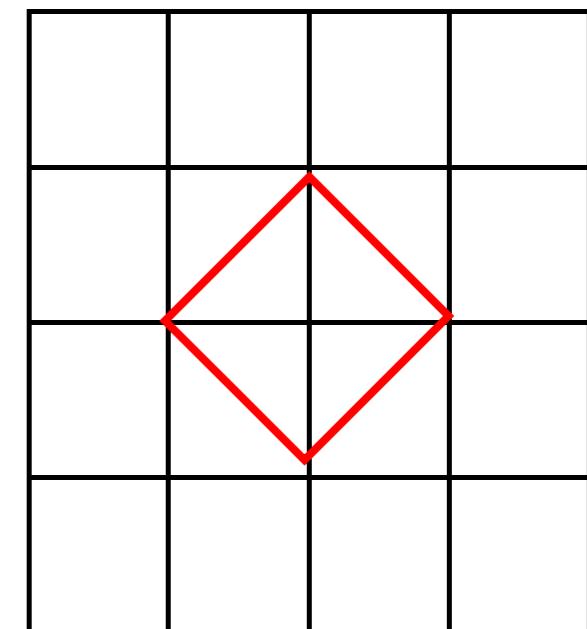
Computational parameters:

$$W_a = 3.6$$

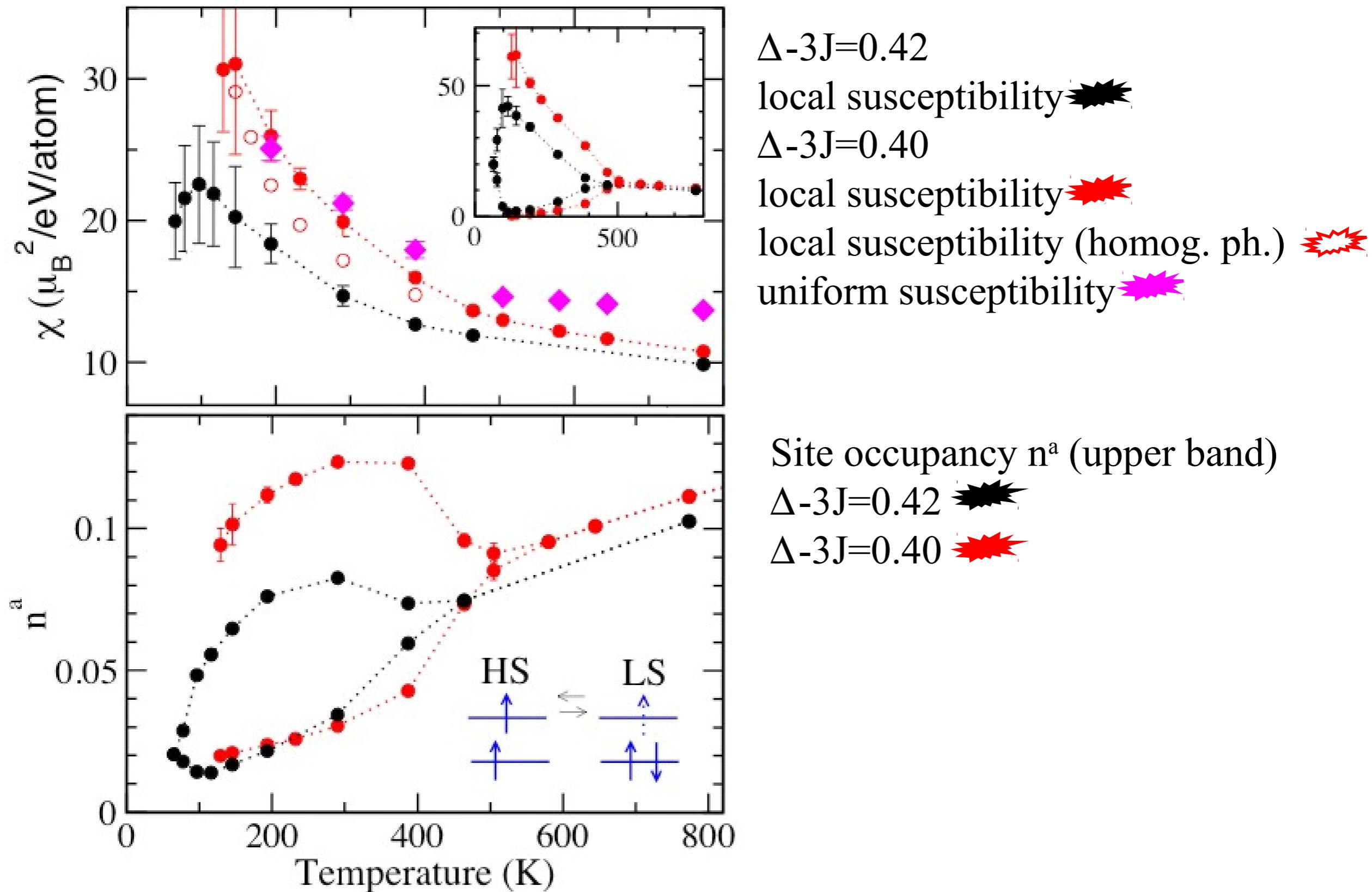
$$W_b = 0.4$$

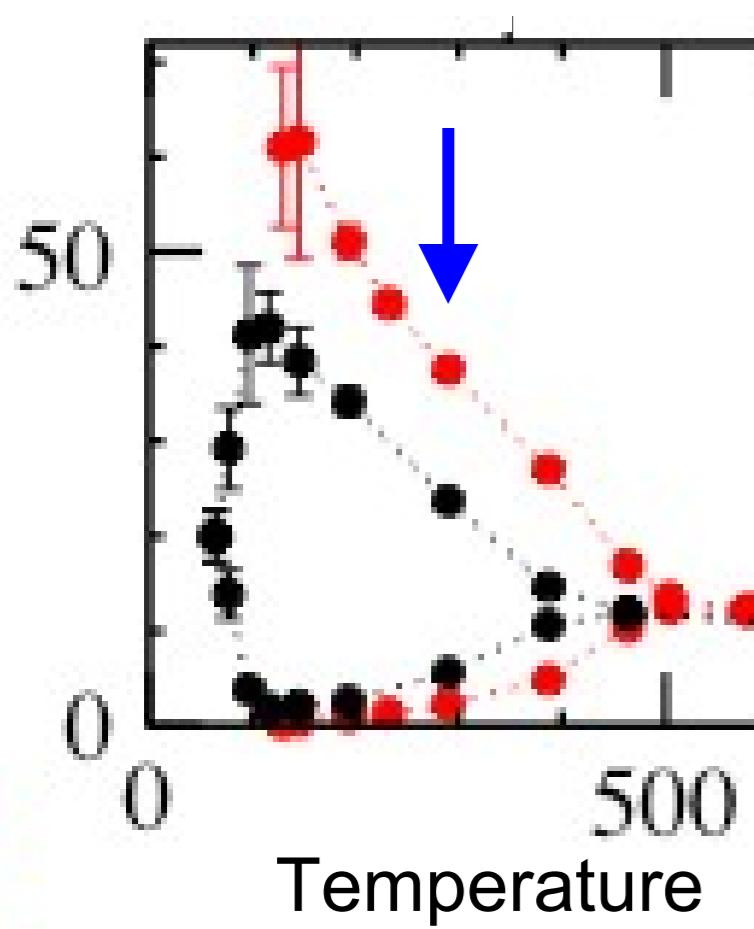
$$U=4, J=1$$

Unit cell:



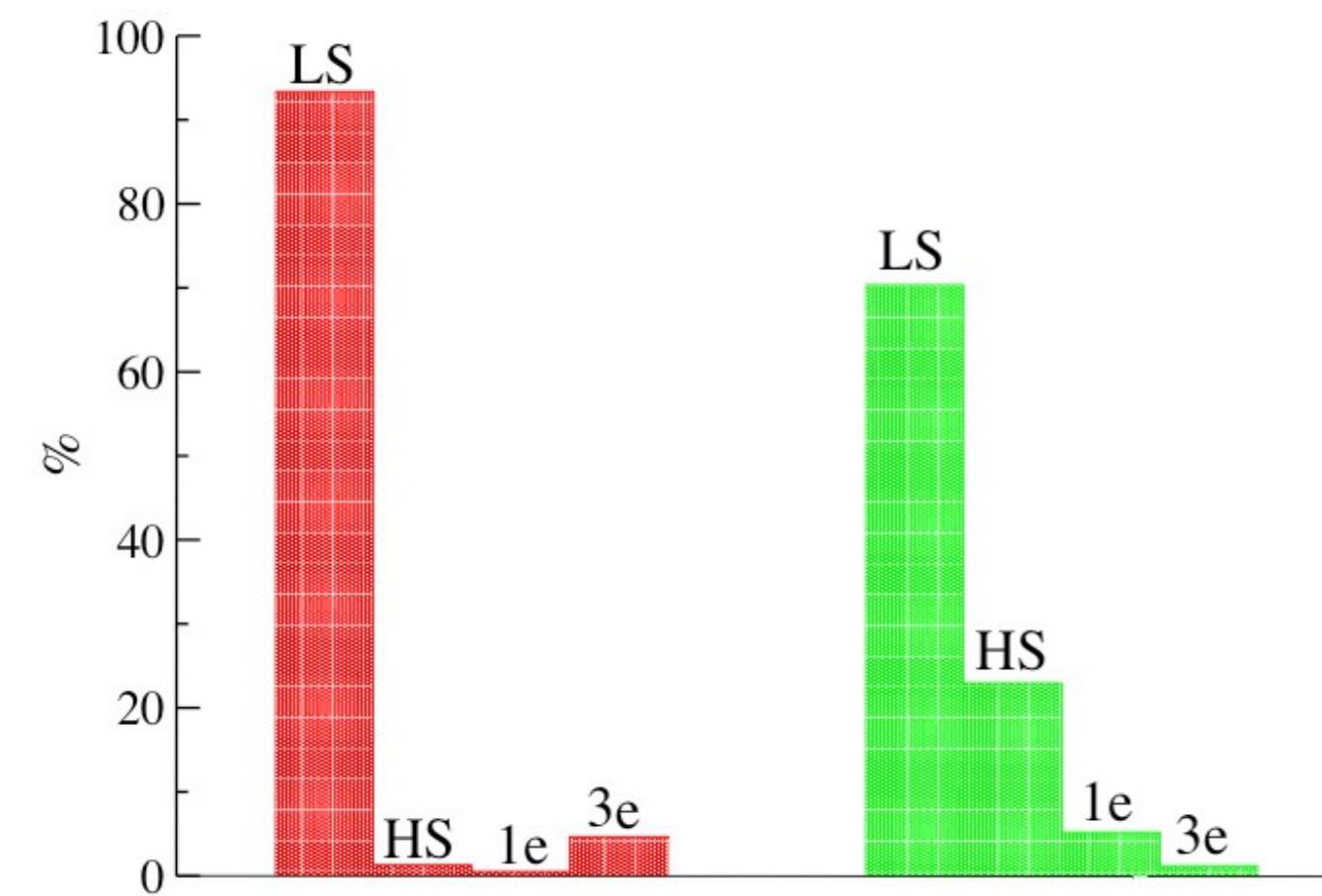
# Spin susceptibility and disproportionation



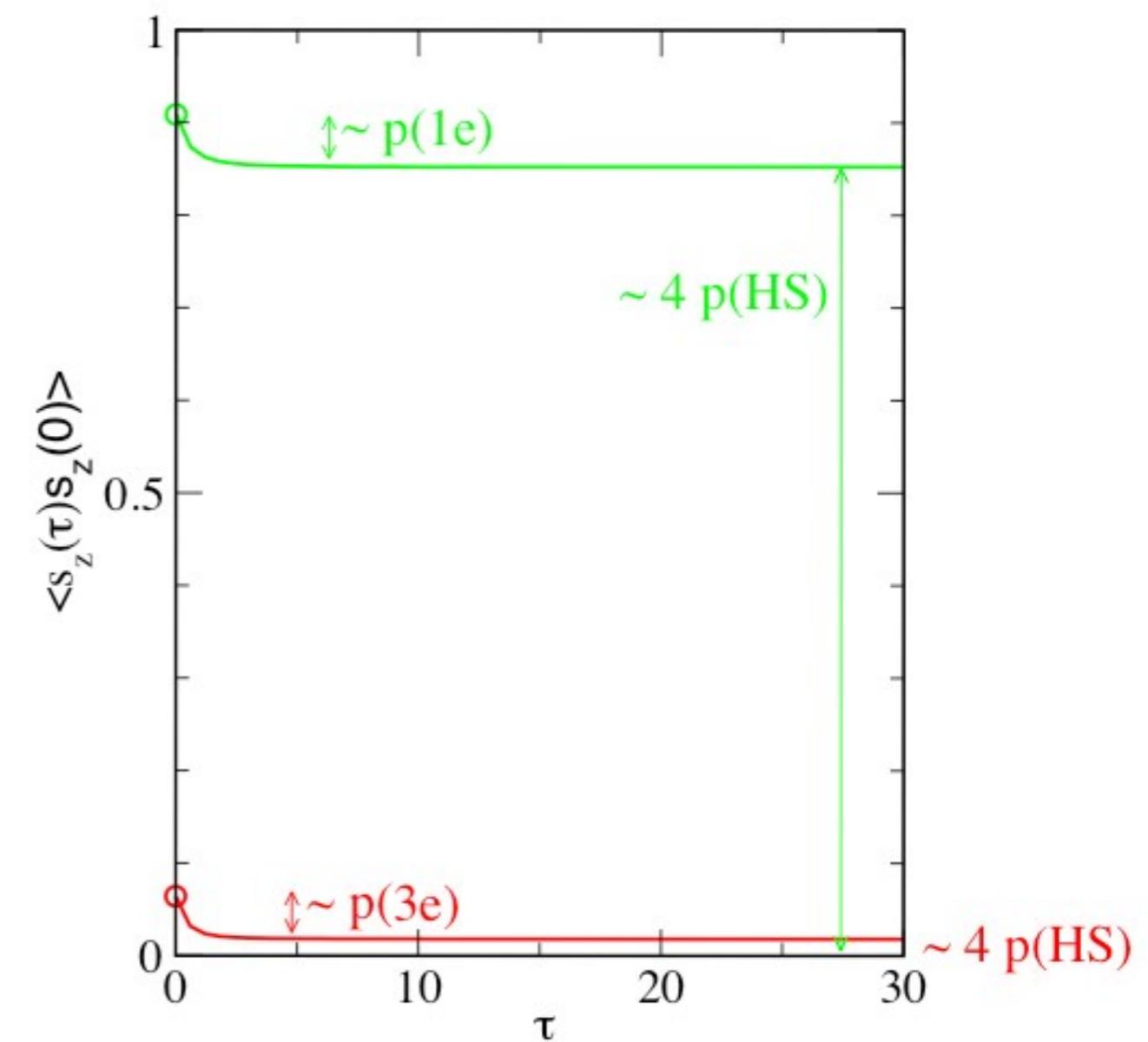


short excursions  
vs  
statistical mixture

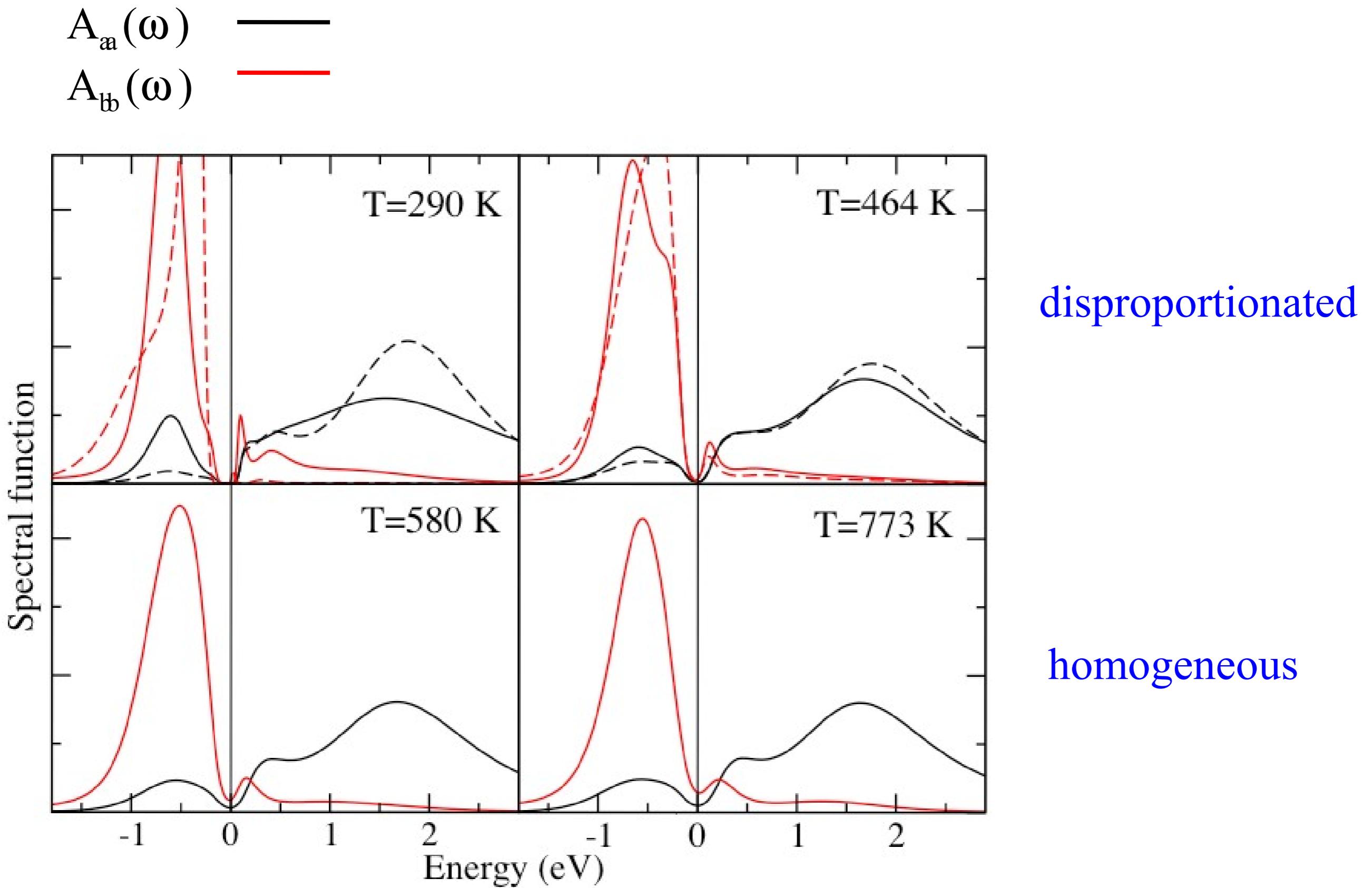
## Local state statistics



## Spin-spin correlations



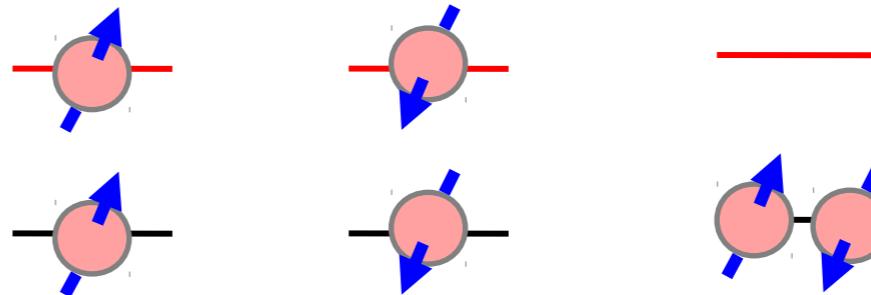
# One-particle spectra



# Low-energy model

Integrate out the charge fluctuations:

- keep 3 local states



- treat hopping as perturbation

Hamiltonian

$$\tilde{H} = \xi_0 \sum_{i,\sigma} n_{i,\sigma}^{\text{HS}} + \sum_{\langle ij \rangle, \sigma} (\xi_1 n_i^{\text{LS}} n_{j,\sigma}^{\text{HS}} + \xi_2 n_{i,\sigma}^{\text{HS}} n_{j,-\sigma}^{\text{HS}})$$

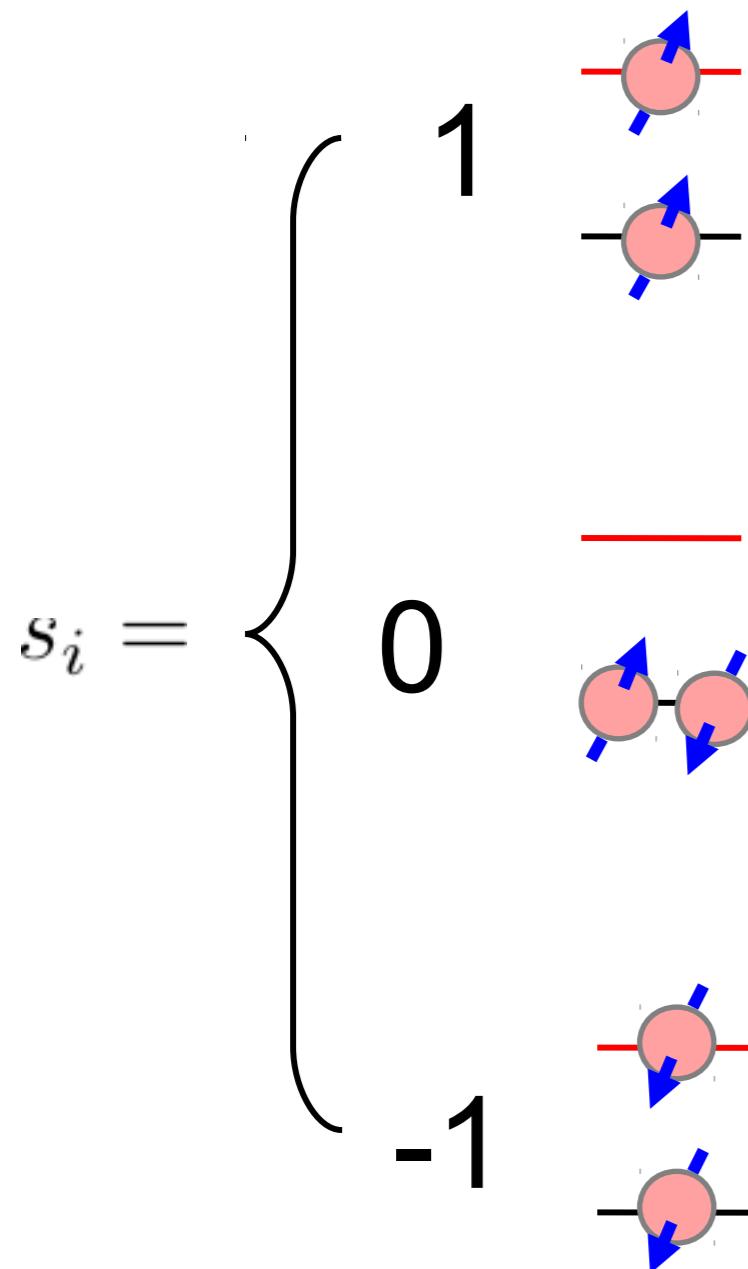
$$\xi_0 = \Delta - 3J, \quad \xi_1 = -\frac{t_{aa}^2}{U-2J}, \quad \xi_2 = -\frac{2t_{aa}^2}{U+J}$$

Mean-field free energy

$$\begin{aligned} F(T) &= \frac{\xi_0}{2}(x_A + x_B) + 2\xi_1(x_A + x_B - 2x_A x_B) - \xi_2 x_A x_B \\ &+ \frac{T}{2}(1 - x_A) \ln(1 - x_A) + \frac{T}{2}(1 - x_B) \ln(1 - x_B) \\ &+ \frac{T}{2}x_A \ln\left(\frac{x_A}{2}\right) + \frac{T}{2}x_B \ln\left(\frac{x_B}{2}\right), \end{aligned}$$

# Blume-Emery-Griffiths model

$$\tilde{H} = D \sum_i s_i^2 + K \sum_{\langle ij \rangle} s_i^2 s_j^2 + I \sum_{\langle ij \rangle} s_i s_j$$



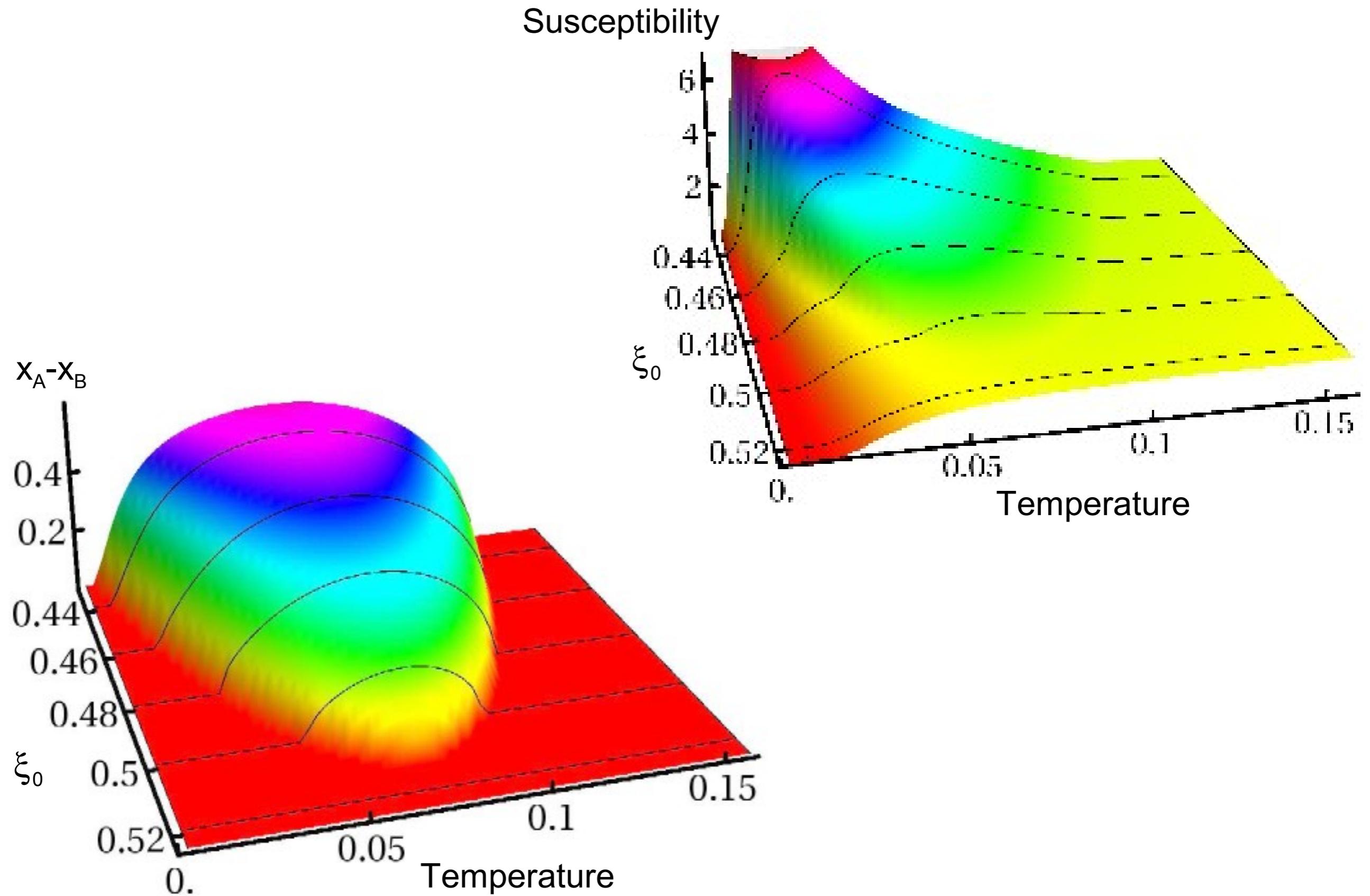
Blume et al., Phys. Rev. A 4, 1071 (1971)

$$D = \Delta - 3J - \frac{Zt^2}{U - 2J}$$

$$K = t^2 \left( \frac{1}{U - 2J} - \frac{1}{U + J} \right)$$

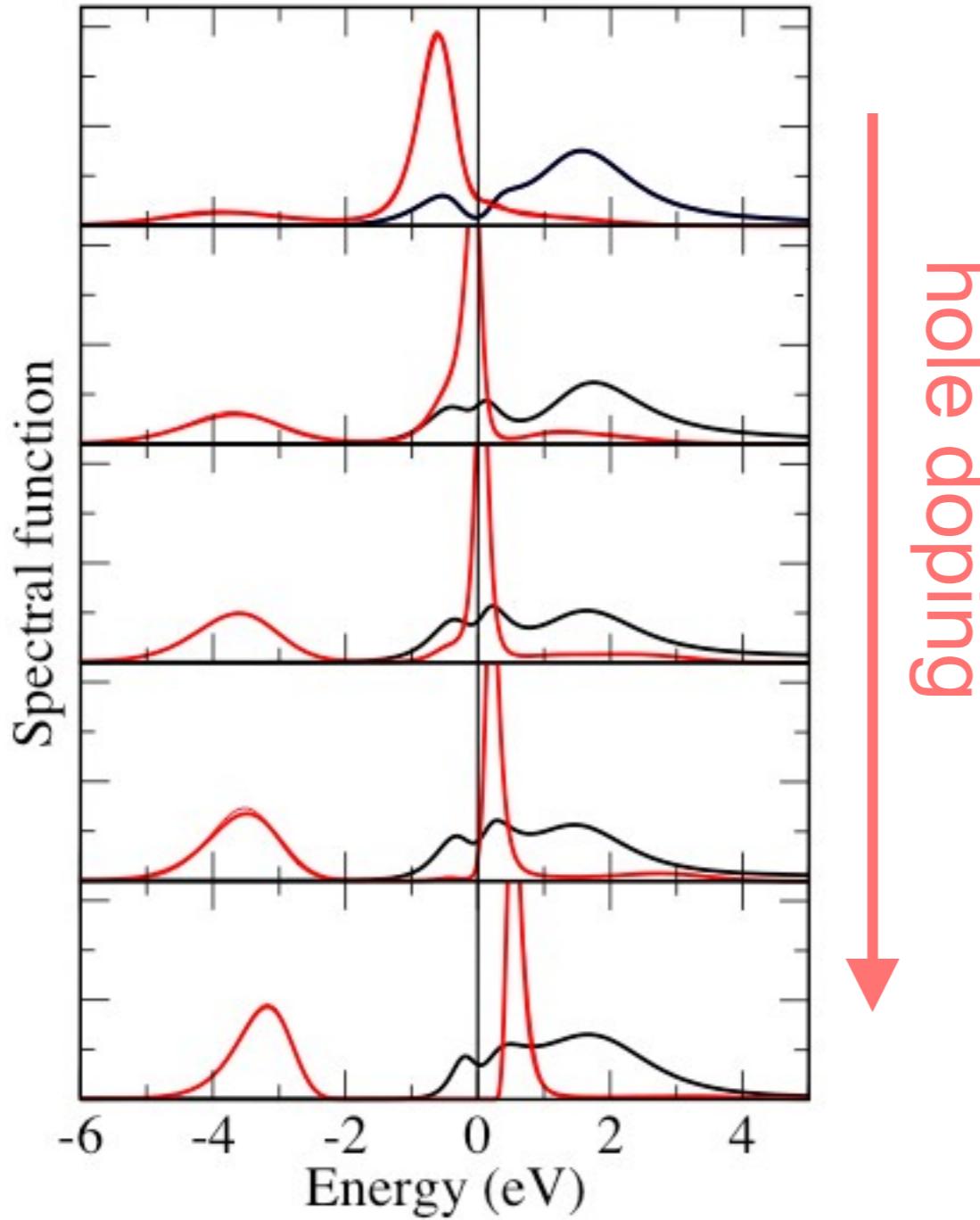
$$I = \frac{t^2}{U + J}$$

# Low-energy model

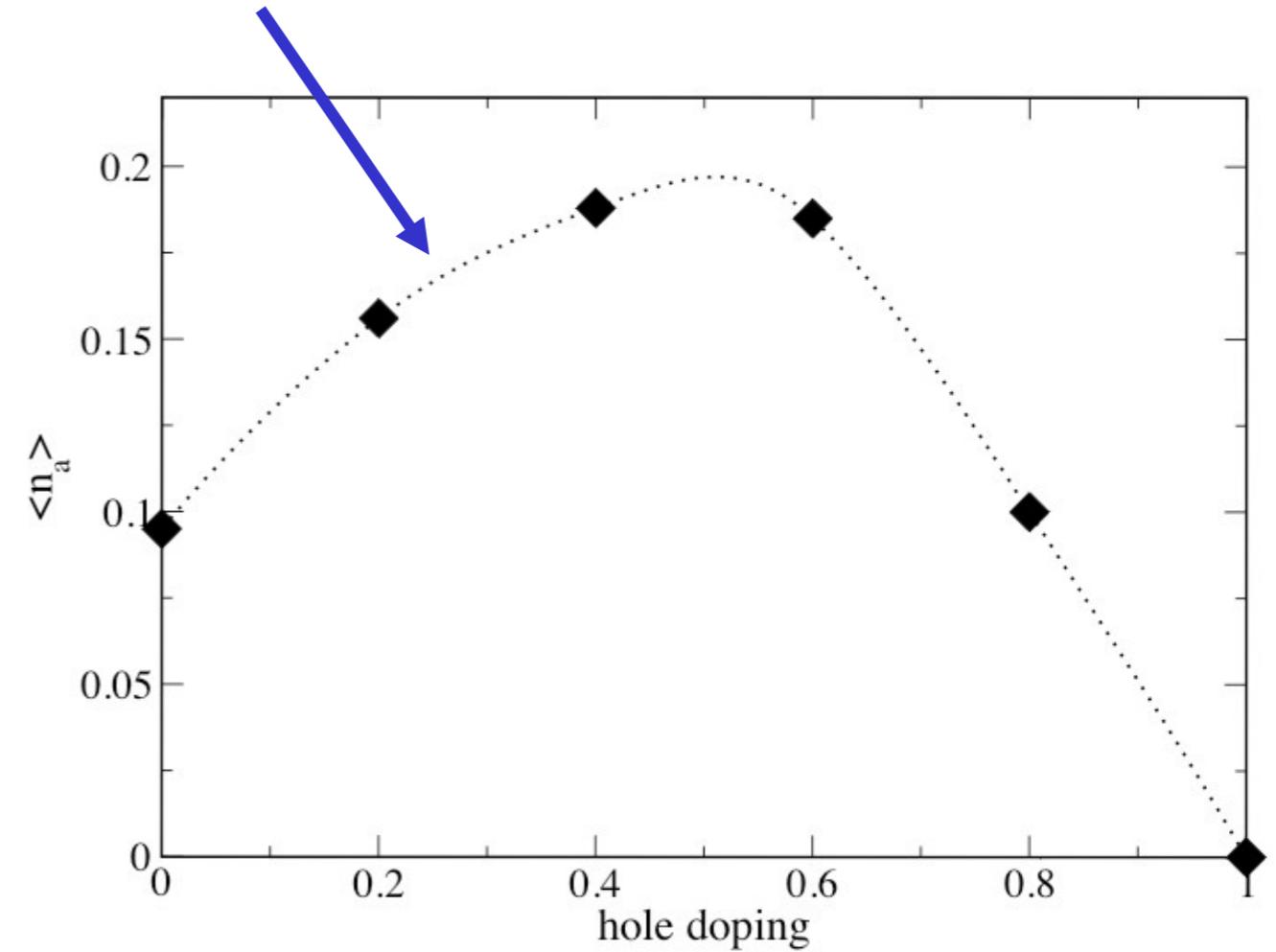


# Hole doping

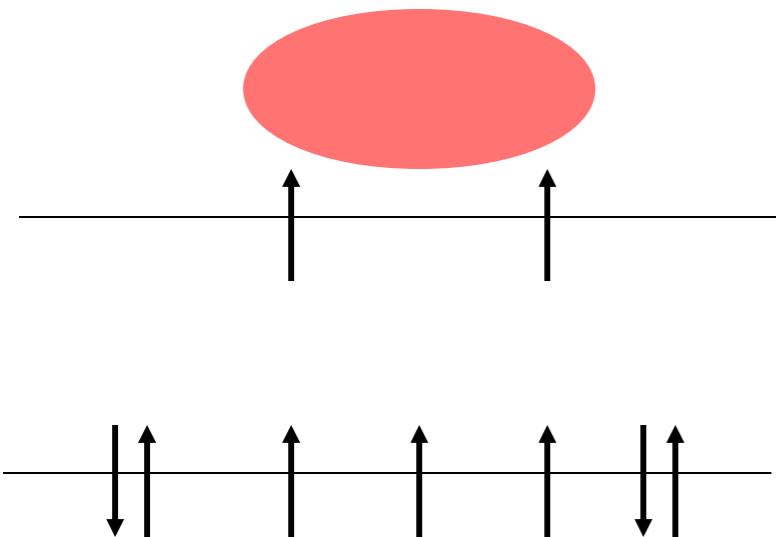
How do we from localized moments to double exchange picture?



Upper band occupancy increases !

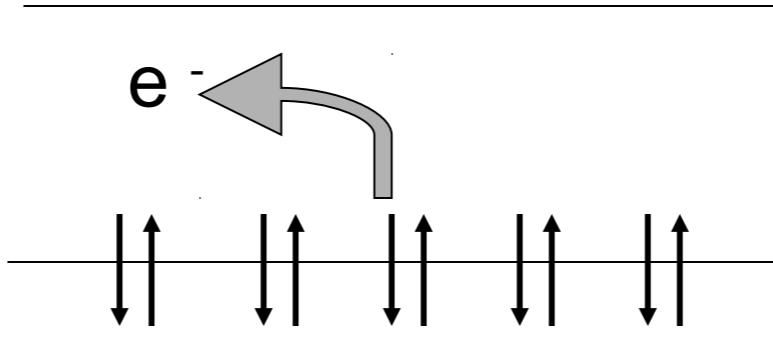


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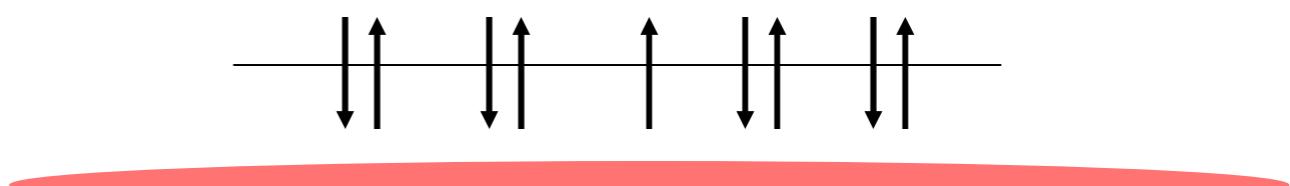


$$\sim -\sqrt{2}t_a + 2\xi_0$$

localized magnetic polaron



OR



$$\sim -2t_b$$

itinerant hole in lower band

# Conclusions

- (Quasi)degeneracy of ionic multiplets leads to rich phase diagrams in strongly correlated systems.
- Effective HS-LS attraction at the HS/LS transitions leads to a ordered state with reduced translational symmetry.
- 2-band Hubbard model with crystal field provides fermionic realization of BEG model and introduces new parameter - doping
- Under certain circumstances ( $W_a \gg W_b$ ) doping leads to formation of inhomogeneities - magnetic polarons